

Time series classification at scale

François Petitjean

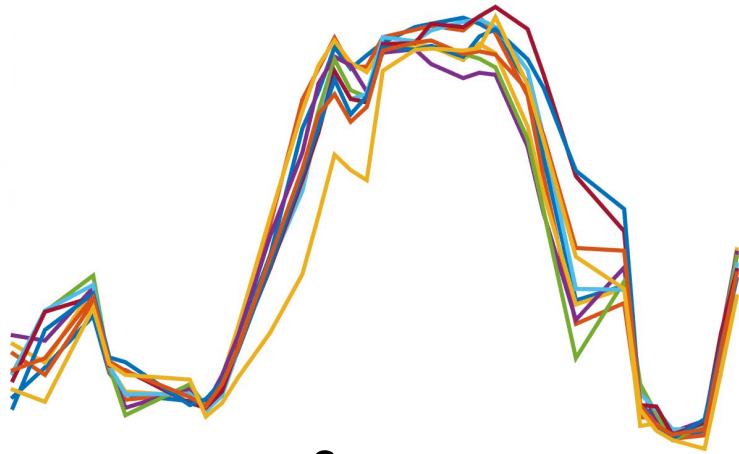
<http://francois-petitjean.com>

PhD work of A. Shifaz, B. Lucas and H. Ismail Fawaz

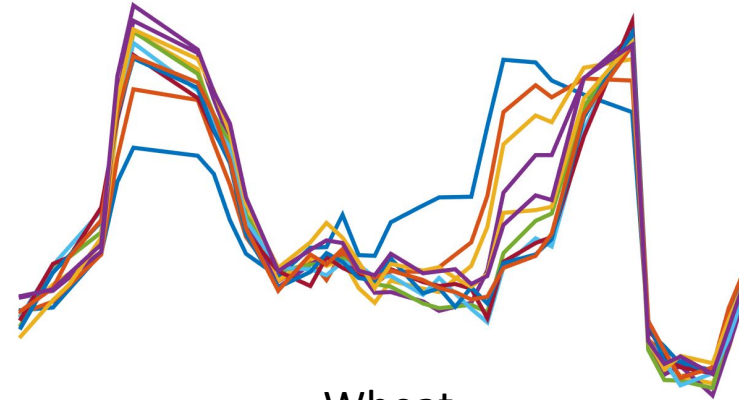
... with G. Forestier, C. Pelletier, G. Webb, J. Weber, B. Goethals, J. Weber, D. Schmidt, L. Idoumghar, P. Muller, L. O'Neill, and N. Zaidi



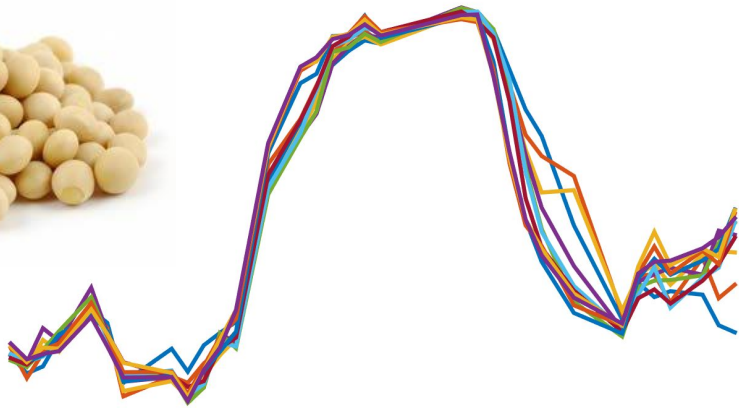
Time series classification



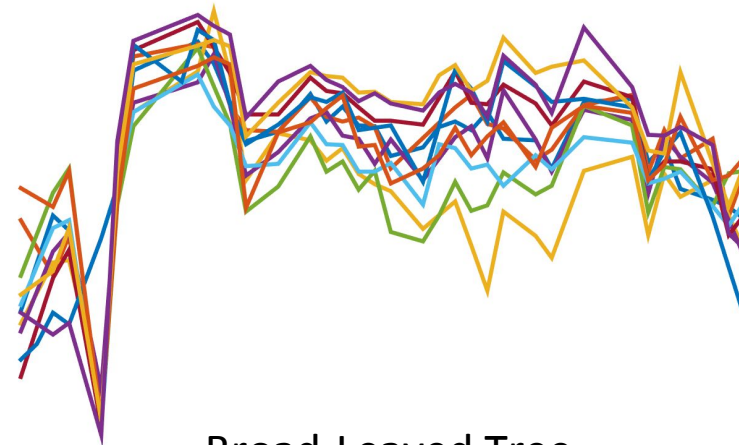
Corn



Wheat



Soybean



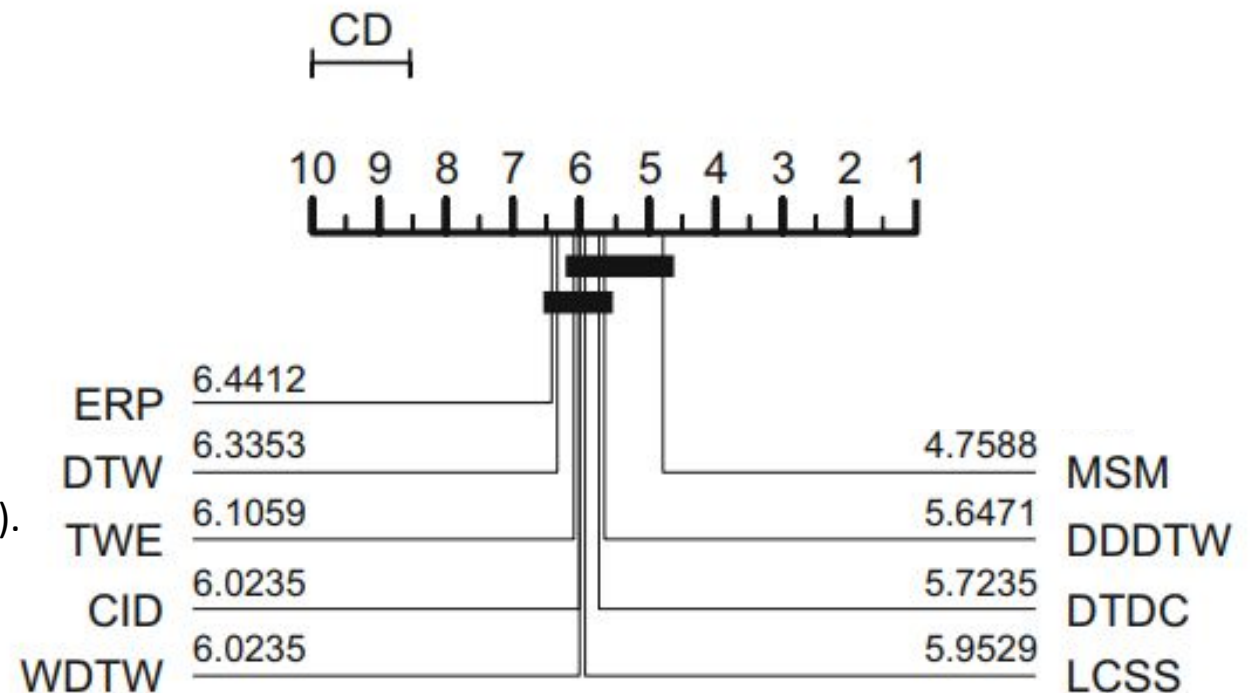
Broad-Leaved Tree



Research into time series classification has accelerated very quickly over the last 5 years

Until recently,

- Many specialised time series classifiers developed
- But none dominated on accuracy on the UCR repository (85 datasets)

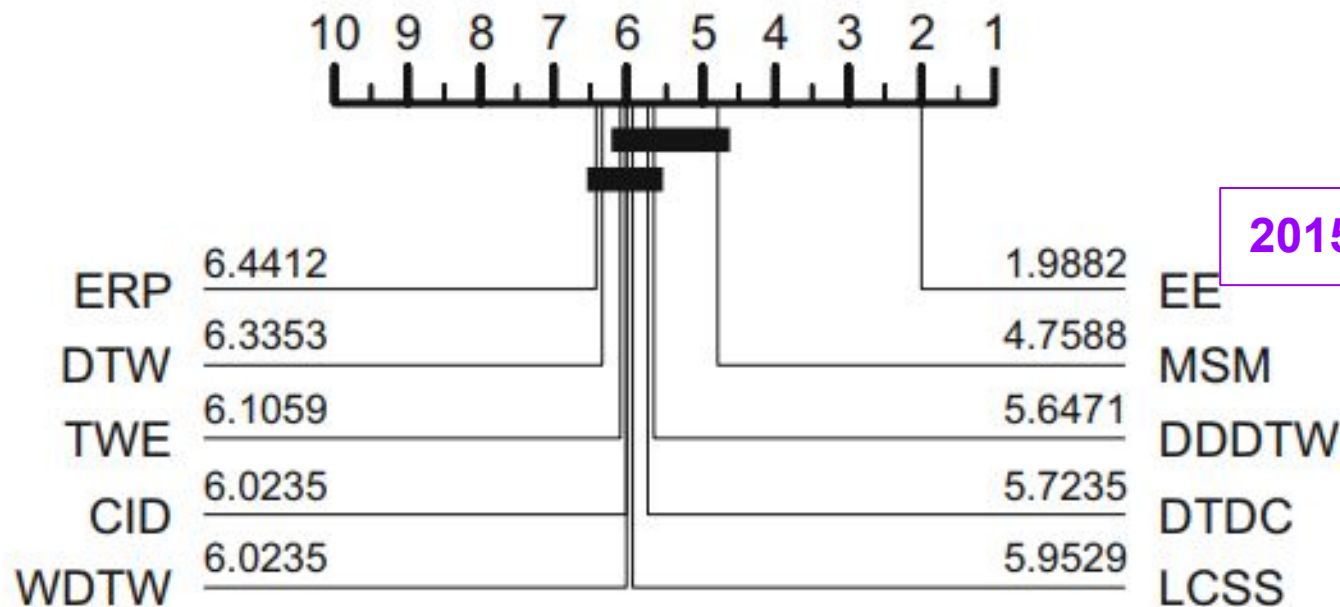


Bagnall, A., Lines, J., Bostrom, A., Large, J., & Keogh, E. (2017). The great time series classification bake off: a review and experimental evaluation of recent algorithmic advances. *Data Mining and Knowledge Discovery*, 31(3), 606-660.

A revolution in time series classification

Ensembles* have swept all before them!

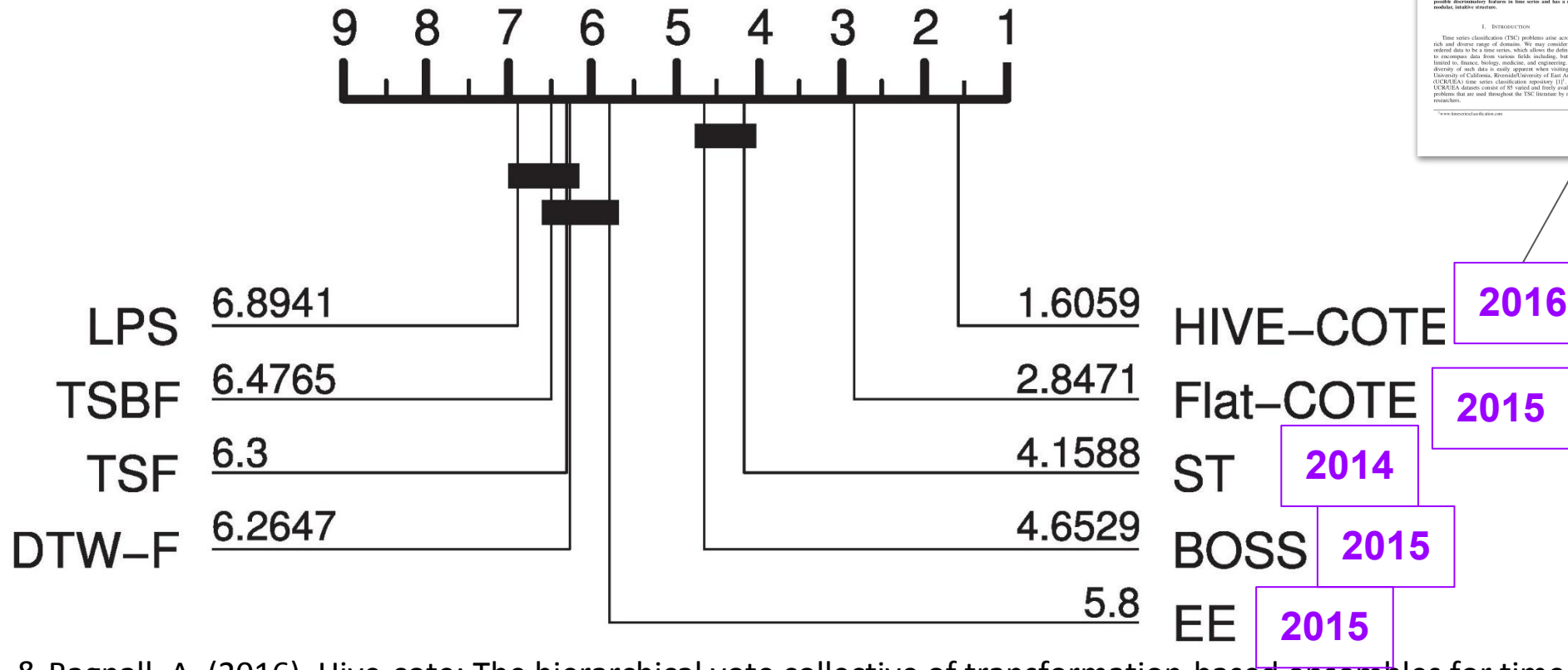
* i.e. Tony, Jason, James and Aaron :)



Lines, J. & Bagnall, A., Time Series Classification with Ensembles of Elastic Distance Measures, *Data Mining and Knowledge Discovery*, 2015.

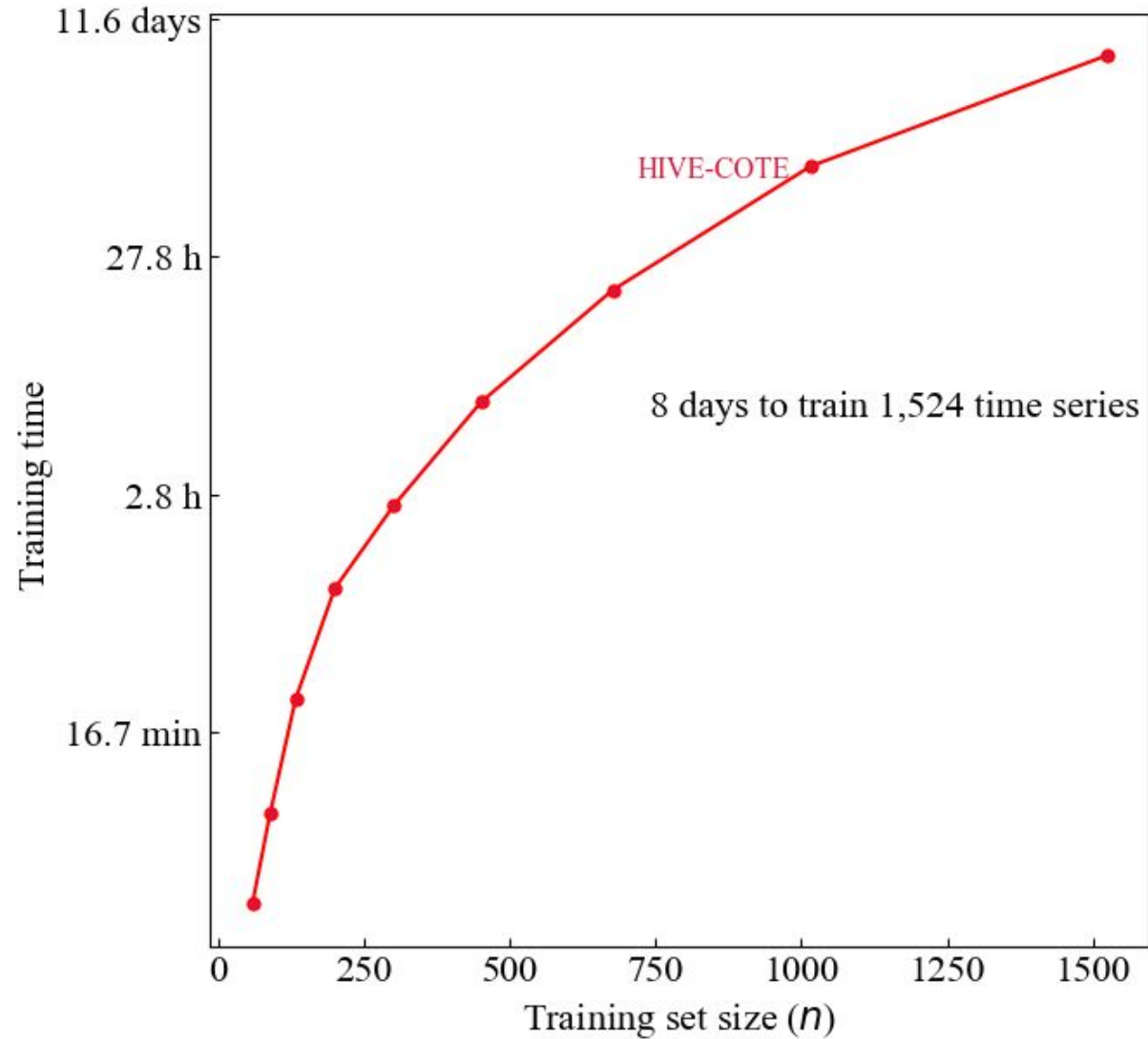
A revolution in time series classification

They didn't stop there: a leap forward around 2015



Lines, J., Taylor, S., & Bagnall, A. (2016). Hive-cote: The hierarchical vote collective of transformation-based ensembles for time series classification. In *2016 IEEE 16th international conference on data mining (ICDM)* (pp. 1041-1046). IEEE.

However, the most accurate ensembles do not scale



State-of-the-art methods

Historical baseline

- ▶ 1-NN with Dynamic Time Warping (DTW)
[Ratanamahatana and Keogh, 2005 ; Ding *et al.*, 2008]
- ▶ window size set by cross-validation

Training time complexity

(n training time series of length l)

$$O(n^2 l^3)$$

Four leading classification algorithms [Bagnall *et al.*, 2017]

- ▶ Bag-Of-SFA-Symbols (BOSS) [Schäfer, 2015]
- ▶ Shapelet Transform (ST) [Hills *et al.*, 2014]
- ▶ Elastic Ensembles (EE) [Lines and Bagnall, 2015]
- ▶ Collective Of Transformation-based Ensembles (COTE)
[Bagnall *et al.*, 2015]

$$O(n^2 l^3)$$

$$O(n^2 l^4)$$

$$O(n^2 l^3)$$

lower bounded by EE and ST algorithms

For 1M training instances, training the EE algorithm would require 73,000 days, **200 years!**

However, the most accurate ensembles do not scale

2017

A. Bagnall et al.



Overall, our results indicate that COTE is, on average, clearly superior to other published techniques. It is on average 8% more accurate than DTW. However, COTE is a starting point rather than a final solution. Firstly, the no free lunch theorem leads us to believe that no classifier will dominate all others. The research issues of most interest are what types of algorithm work best on what types of problem and can we tell *a priori* which algorithm will be best for a specific problem. Secondly, COTE is hugely computationally intensive. It is trivial to parallelise, but its run time complexity is bounded by the Shapelet Transform, which is $O(n^2m^4)$ and the parameter searches for the elastic distance measures, some of which are $O(n^3)$. ST and EE are also trivial to distribute, but there is a limit to the number of processors anyone can run in parallel. An algorithm that is faster than COTE but not significantly less accurate would be a genuine advance in the field. Finally, we are only looking at a very restricted type of

Bagnall, A., Lines, J., Bostrom, A., Large, J., & Keogh, E. (2017). The great time series classification bake off: a review and experimental evaluation of recent algorithmic advances. *Data Mining and Knowledge Discovery*, 31(3), 606-660.

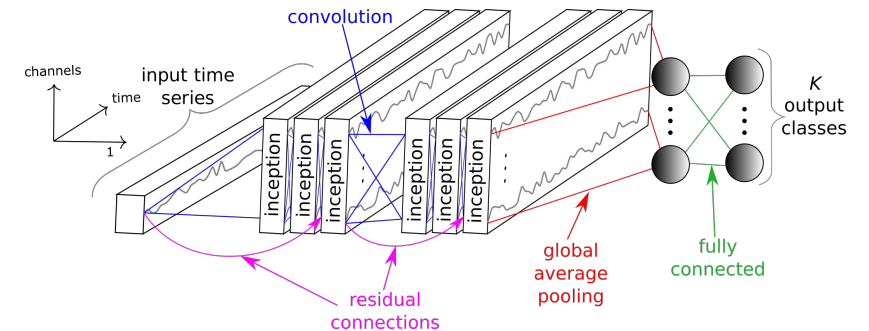
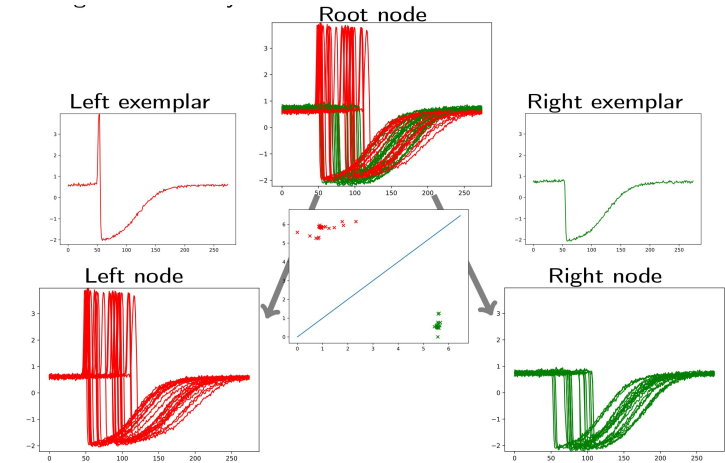
Talk Outline

Highly accurate and scalable TSCs

- Tree-based: *Proximity Forest* and *TS-CHIEF*
- Deep Learning: *InceptionTime*

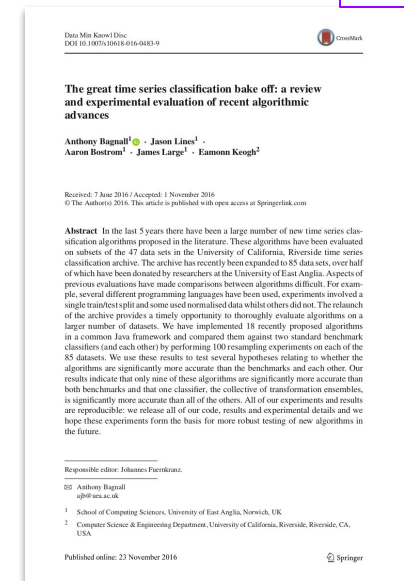
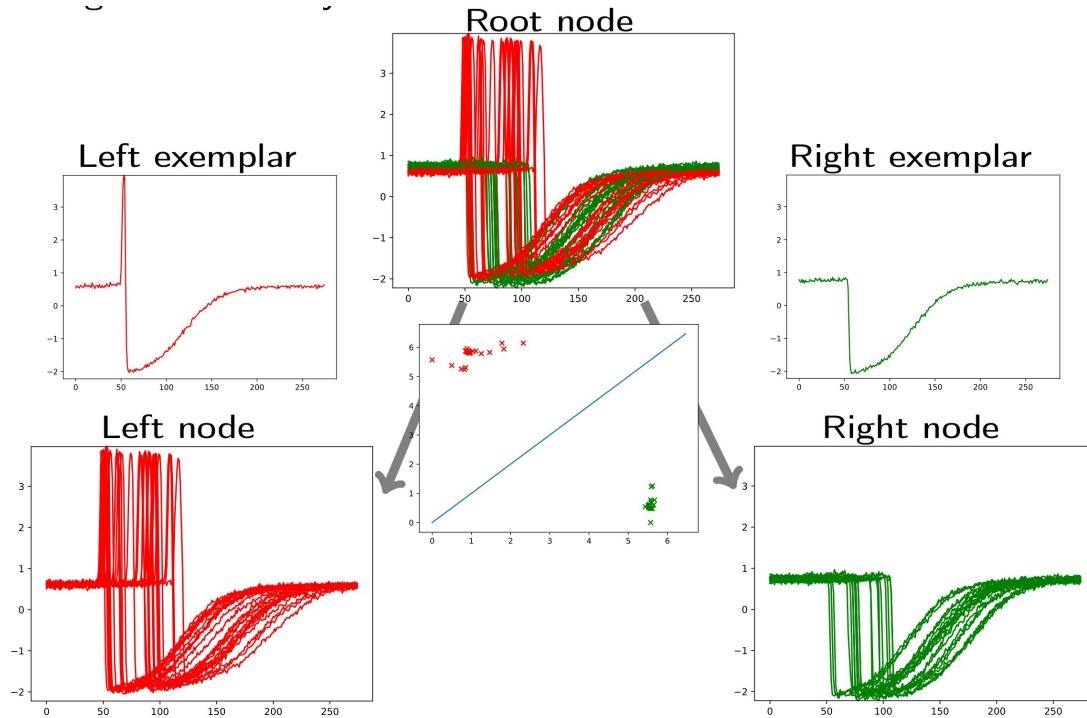
This talk is super fresh!

- 1 DAMI 2019 paper
- 2 arxiv papers submitted in the last 3 months



Part 1: Proximity Forest (PF)

2019



<http://bit.ly/ProximityForest>

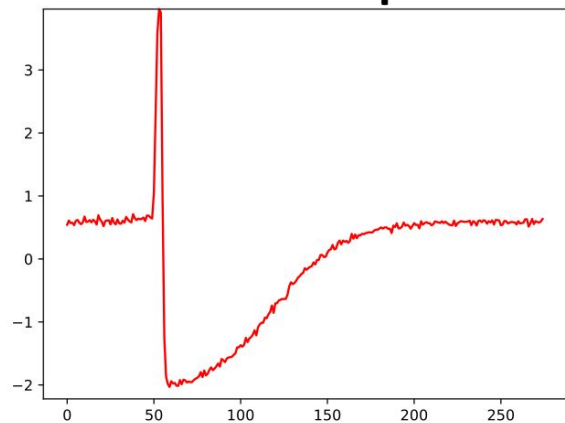
B. Lucas, A. Shifaz, C. Pelletier, L. O'Neill, N. Zaidi, B. Goethals, F. Petitjean, G. Webb (2019). Proximity Forest: An effective and scalable distance-based classifier for time series. *Data Mining and Knowledge Discovery*, 33(3), 607-635.

Proximity Forest

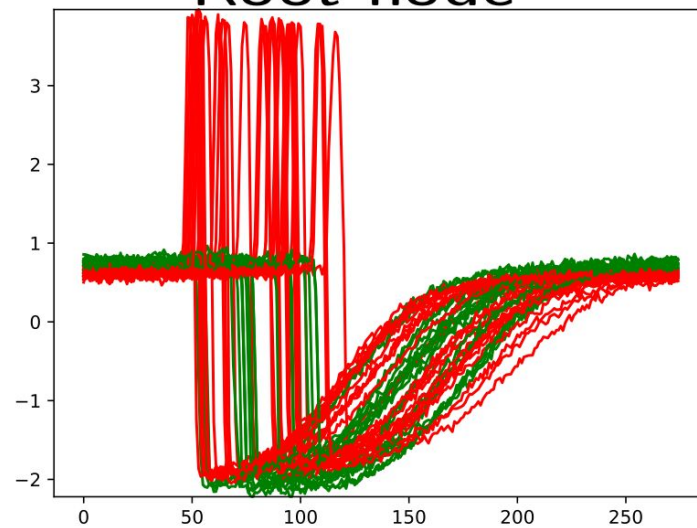
Starting point: How to make Elastic Ensemble (EE) scalable?

- We need a divide-and-conquer approach to be efficient
- We want to emulate Elastic Ensemble as closely as possible to allow clear comparison of fundamental strategies
- But tree-base splits don't work for time series because no attribute/value representation

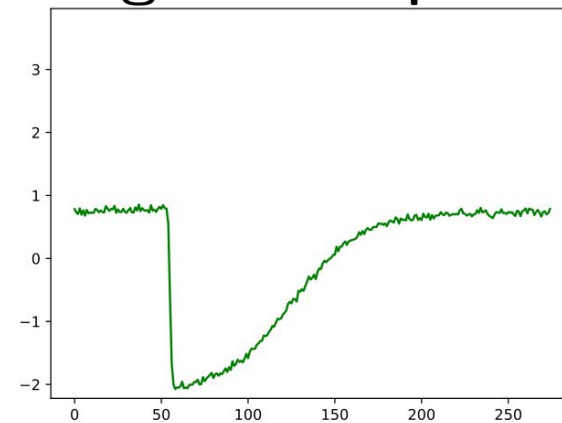
Left exemplar



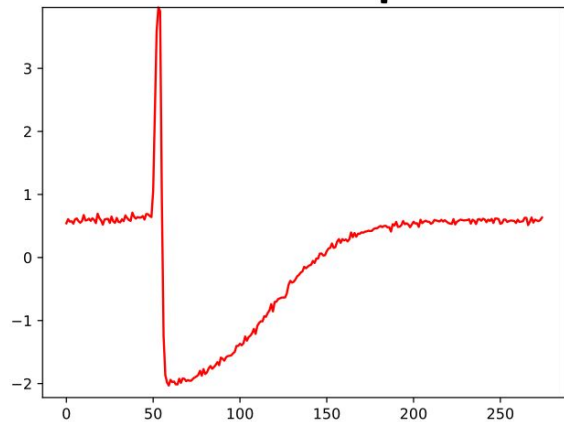
Root node



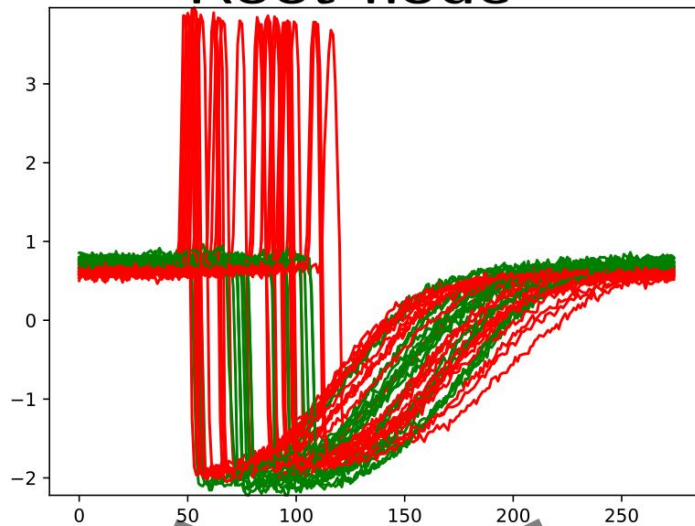
Right exemplar



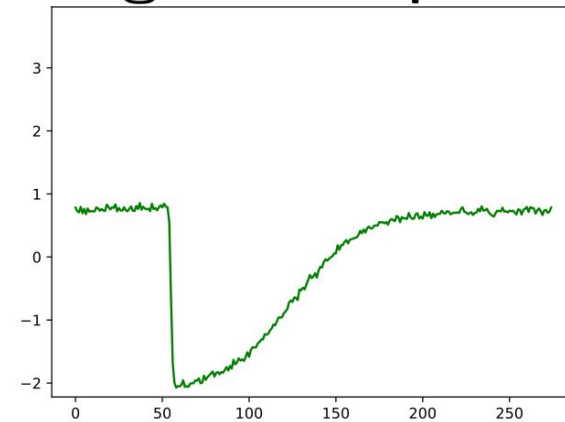
Left exemplar



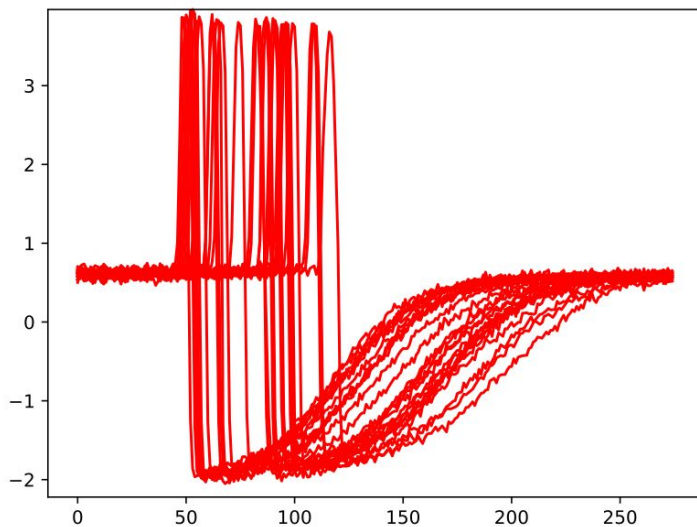
Root node



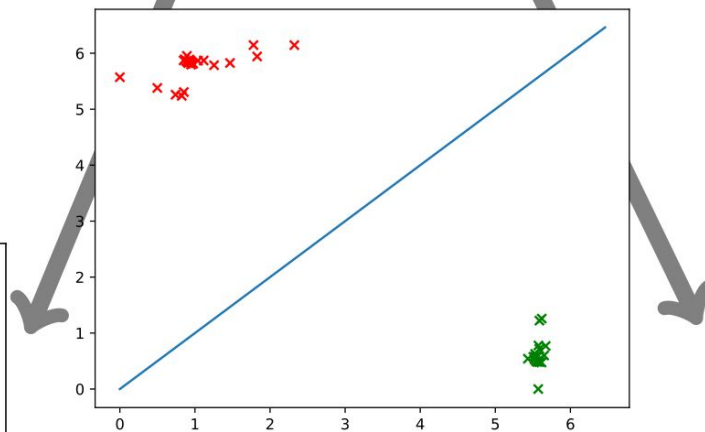
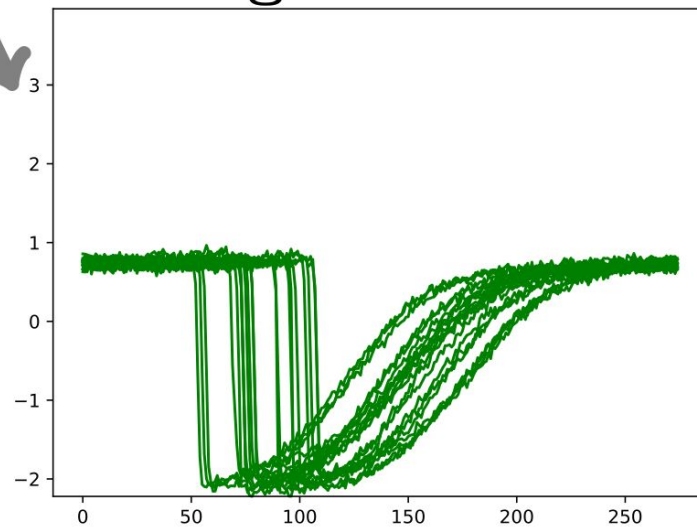
Right exemplar



Left node

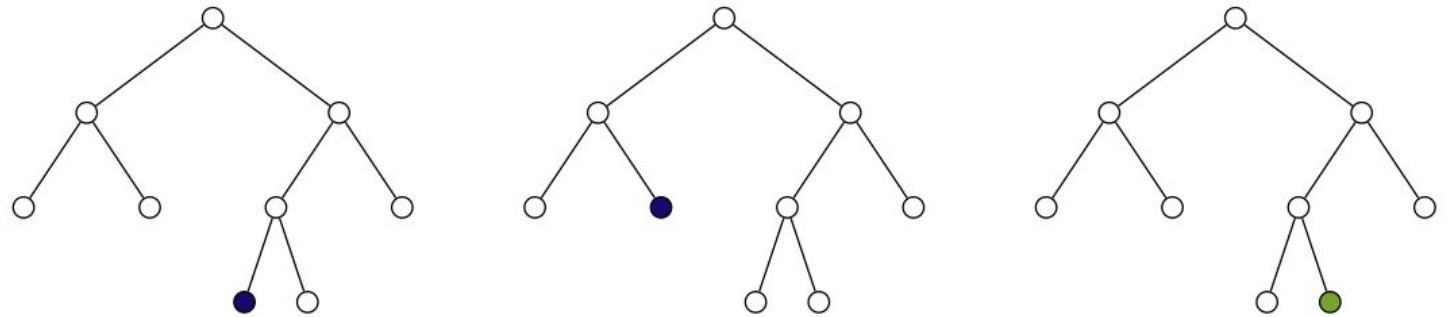


Right node



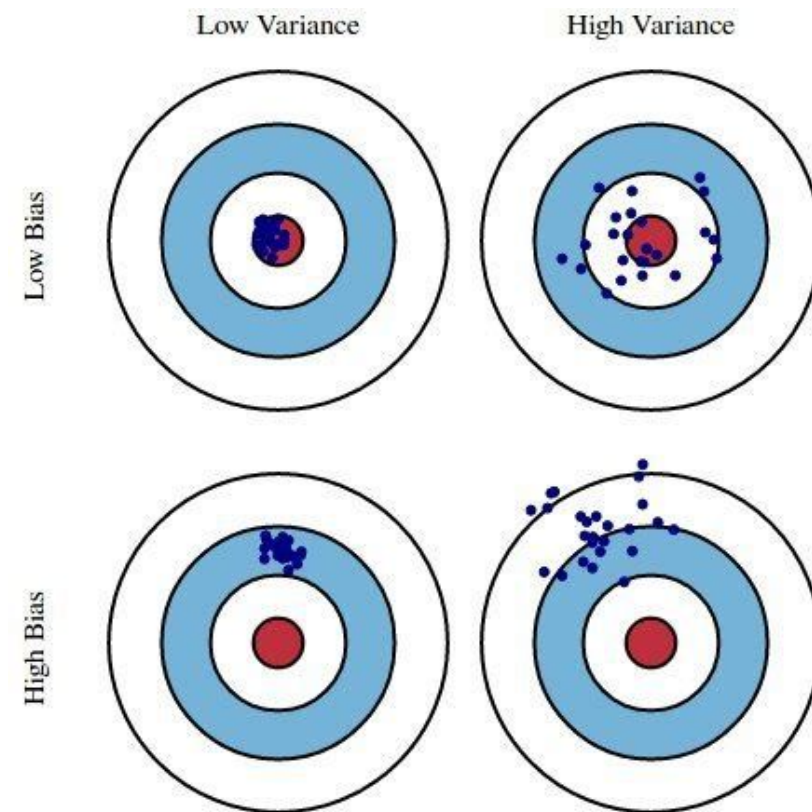
Proximity Tree

- Replace conventional decision tree splits with similarity comparisons using specialised time series methods
 - Makes the most of 40 years of research into designing appropriate measures for time series (DTW, TWE, MSM, LCSS, etc)
- Each branch has an exemplar associated with it
- One exemplar per class
- Each split in the tree has (1) a measure and (2) a parametrization
- For classification, series S_p most similar



Stochastic choices for speed and diversity

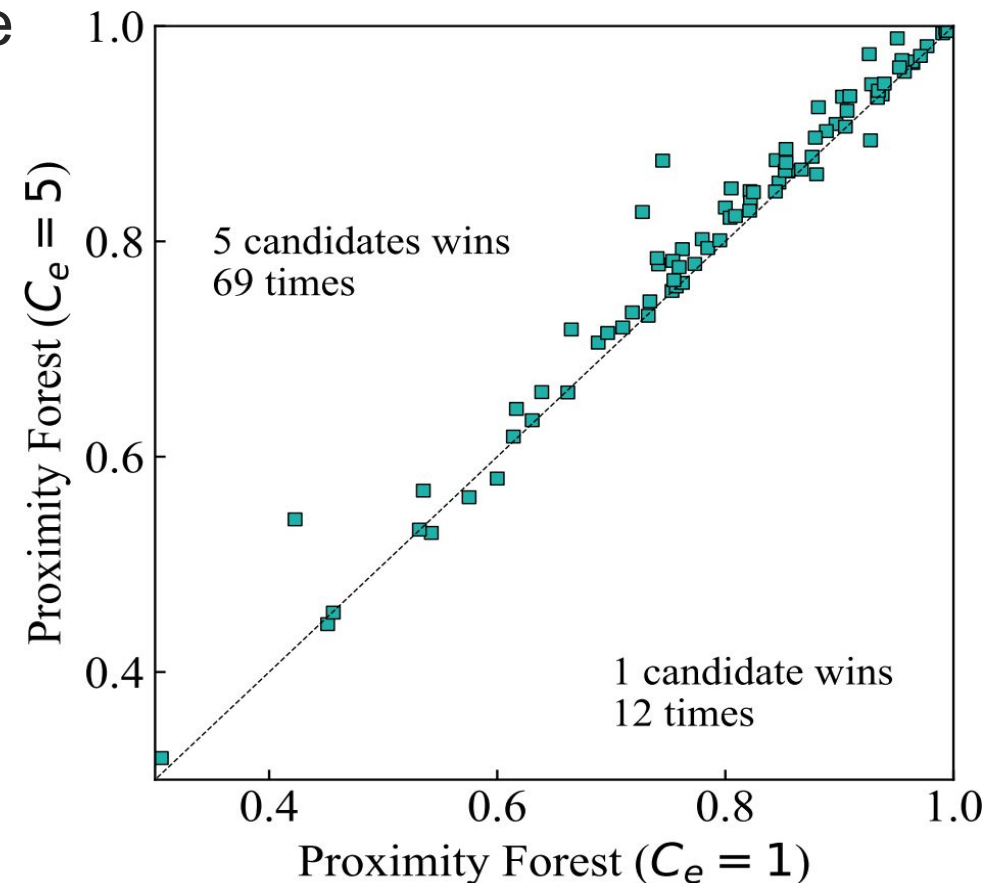
- Exemplars chosen at random among series at the node
- Distance measures and their parameterizations chosen at random from those used by EE
- Random choices have low bias and ensembling removes the resulting variance
- The major training time cost is passing training examples down the tree

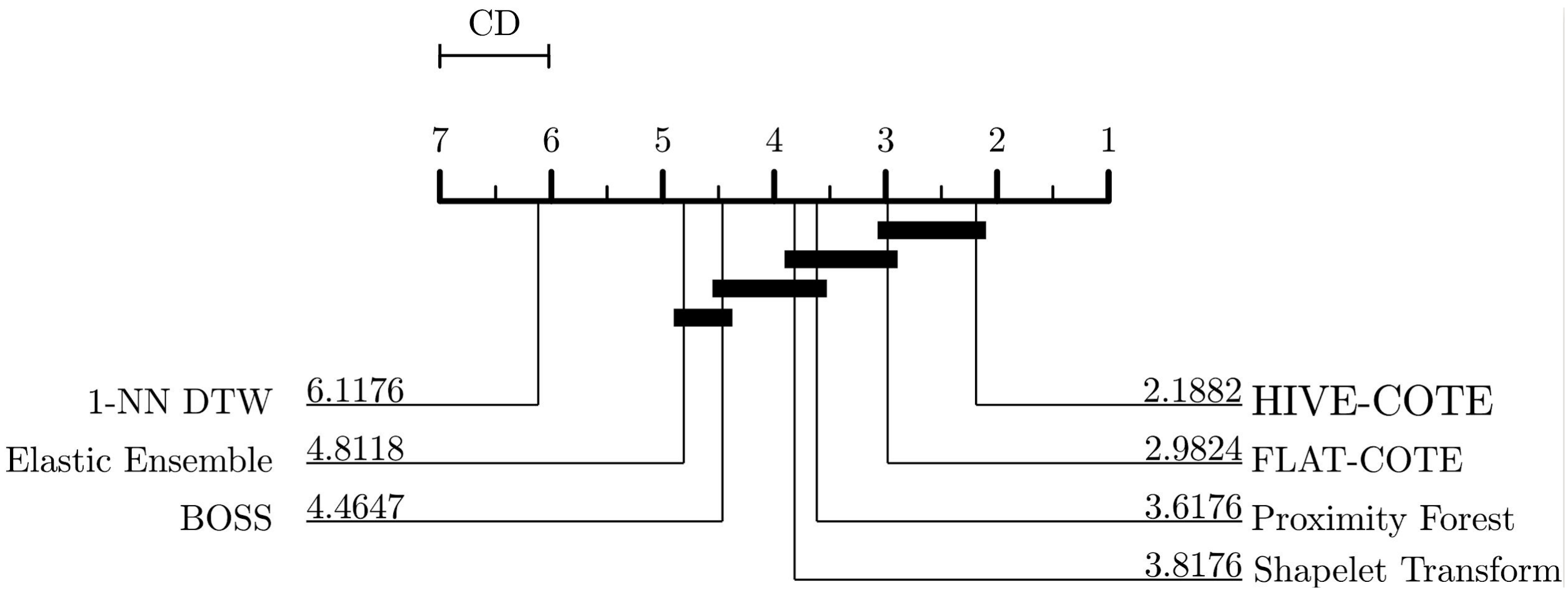


$$\text{MSE}(H) = \overline{bias}(H)^2 + \frac{1}{|H|} \overline{variance}(H) + \left(1 - \frac{1}{|H|}\right) \overline{covariance}(H)$$

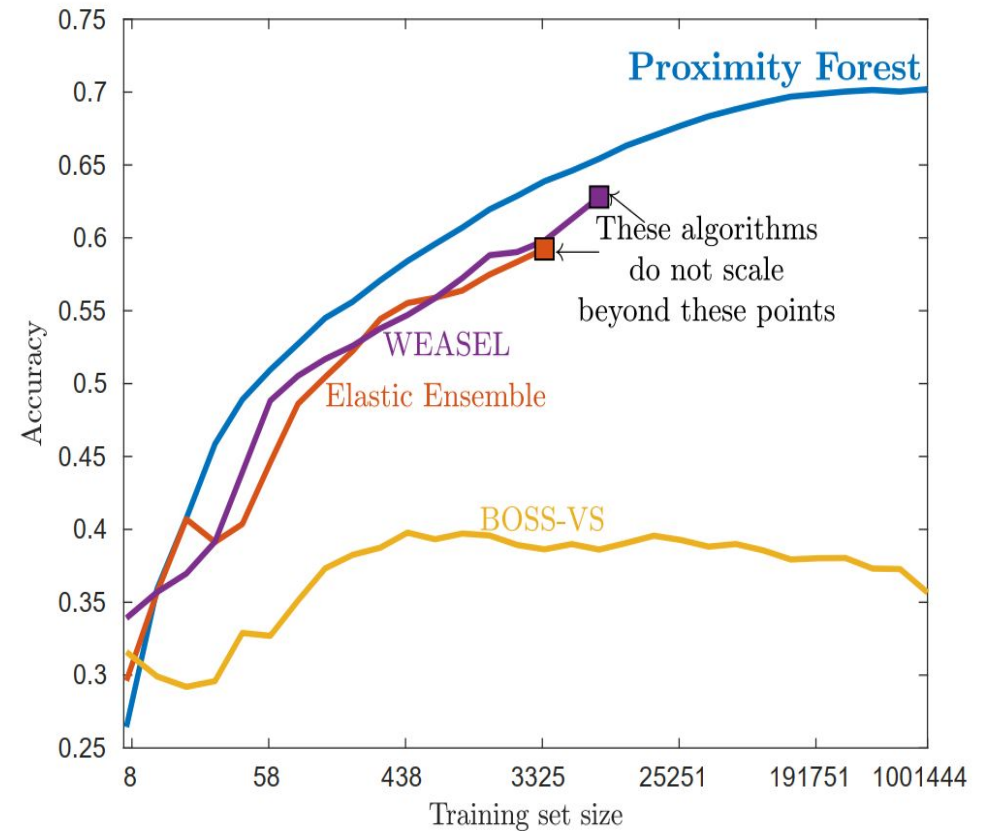
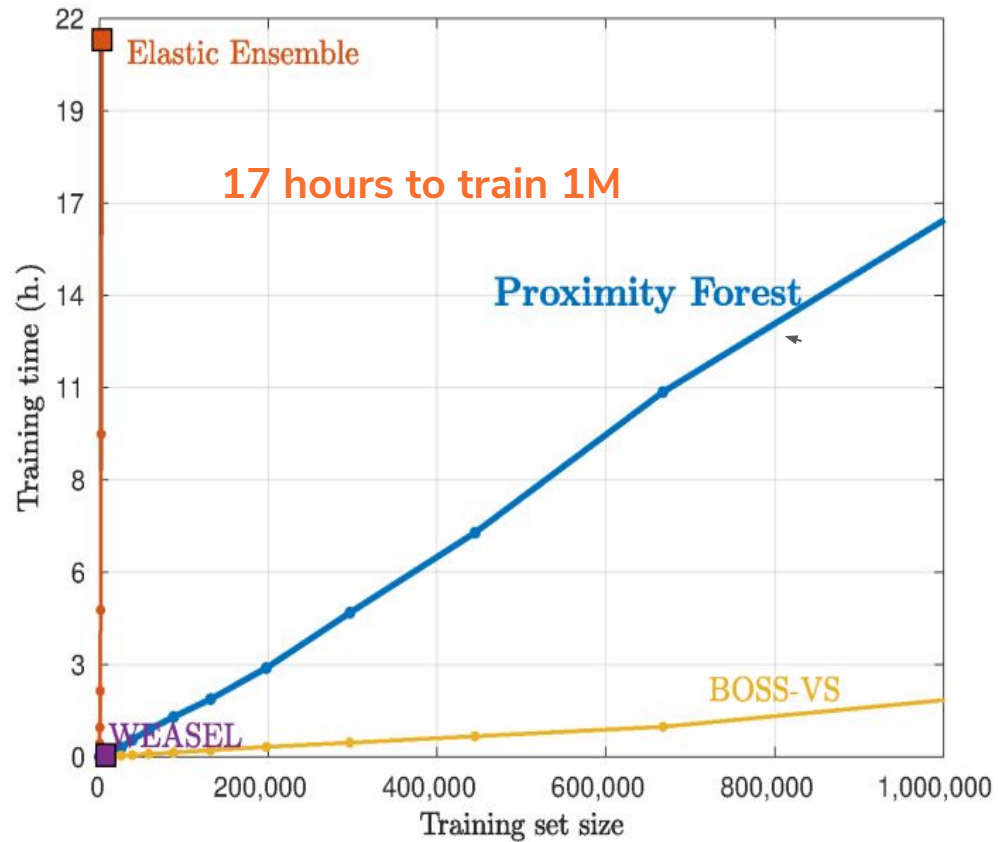
Select between multiple random candidates at each node

- Use GINI to select best from five candidate splits
- Increases covariance, decreases variance
 - so we don't need too many trees
 - faster training
 - faster classification

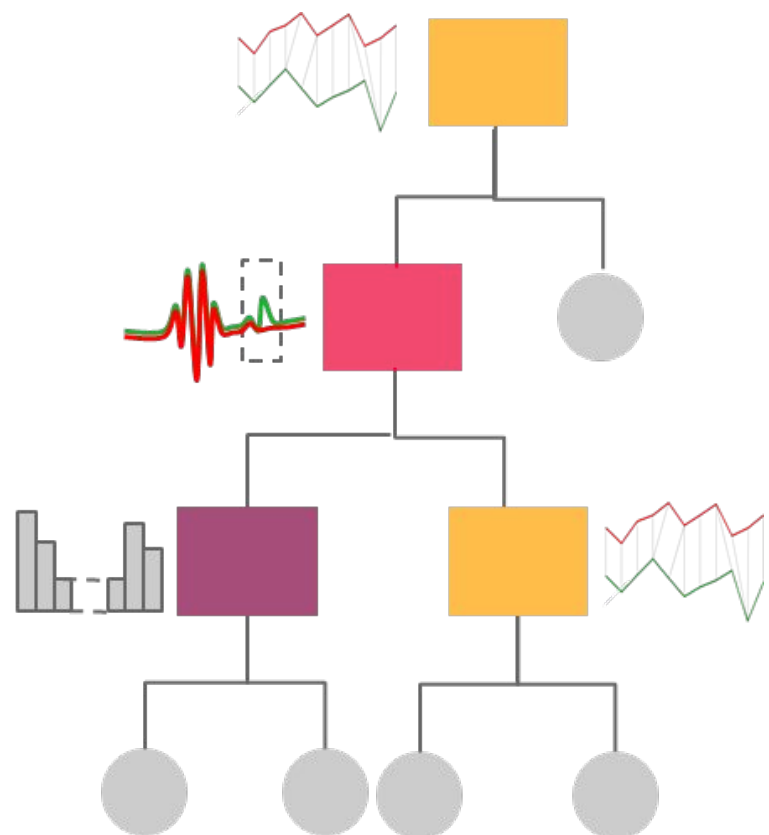




Scalability evaluated on 1M instances of Satellite Image Time Series (SITS) dataset



Part 2: TS-CHIEF



2019 - arxiv

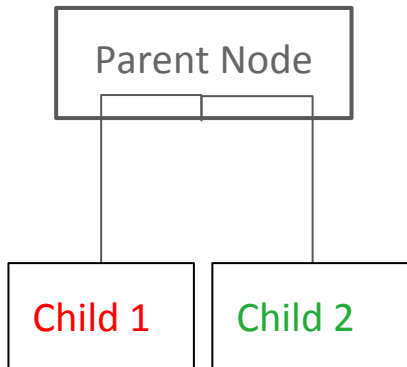


<http://bit.ly/TS-CHIEF>

A. Shifaz, C. Pelletier, F. Petitjean and G. Webb (2019). TS-CHIEF: A Scalable and Accurate Forest Algorithm for Time Series Classification. *under review*. <https://arxiv.org/abs/1906.10329>

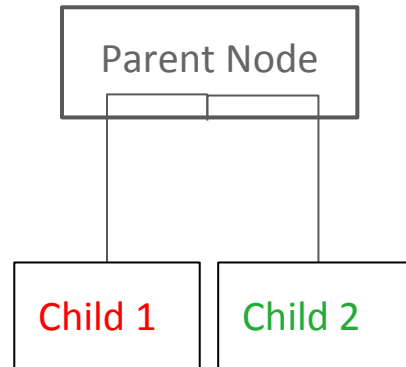
Time Series Combination of Integrated Embeddings Forest (TS-CHIEF)

Similarity-based
(Proximity Forest)



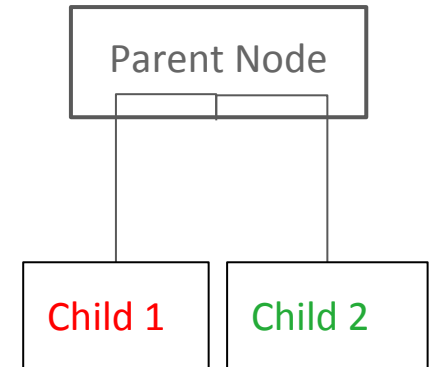
Candidate split 1

Dictionary-based



Candidate split 2

Interval-based



Candidate split 3

- Candidates selected at random from all three strategies
- Selection using Gini Index

Time Series Combination of Heterogeneous Integrated Embeddings Forest (TS-CHIEF)

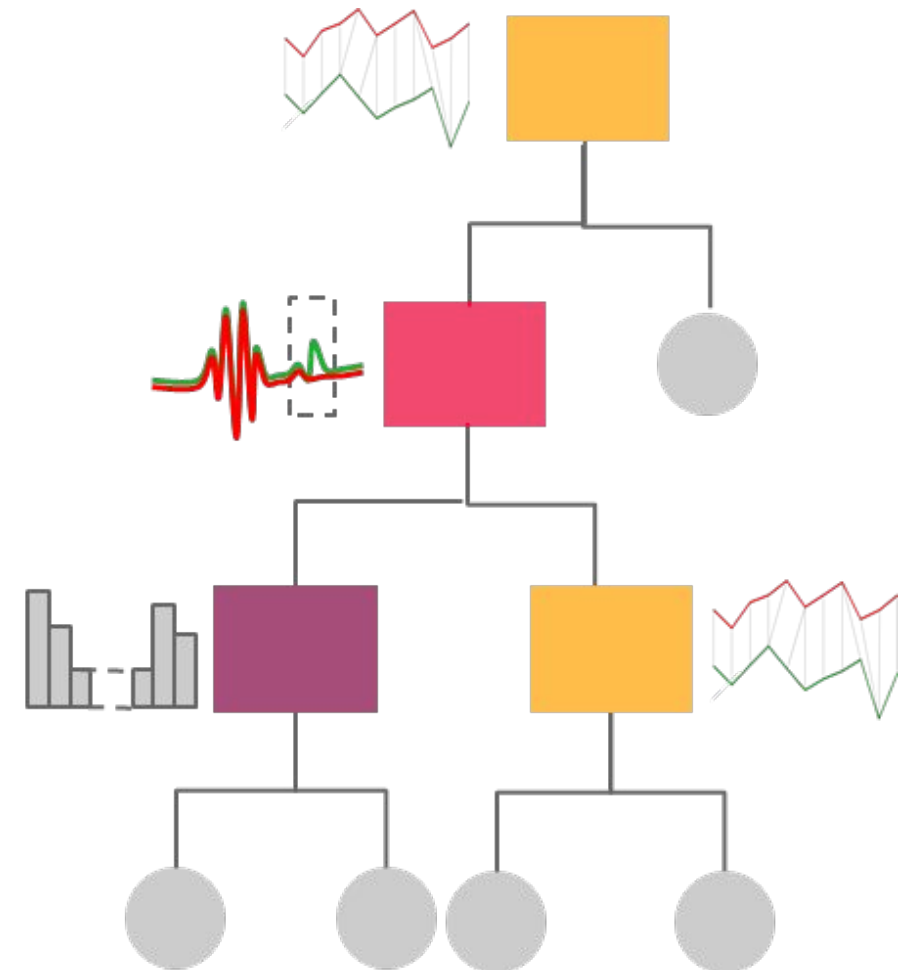
- TS-CHIEF trees combine three splitting functions
- Candidate splits selected at random
- Final selection using Gini Index

 Similarity-based internal node

 Interval-based internal node

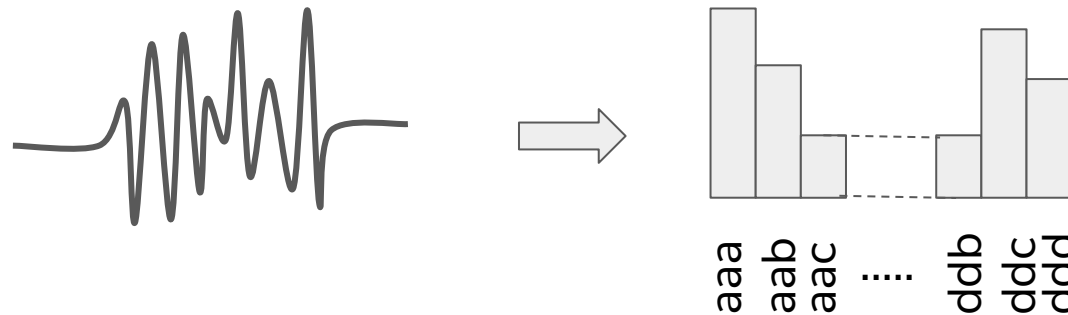
 Dictionary-based internal node

 Leaf Node



TS-CHIEF : Dictionary-based splitter

- Precomputes a pool of BOSS transformations at forest level



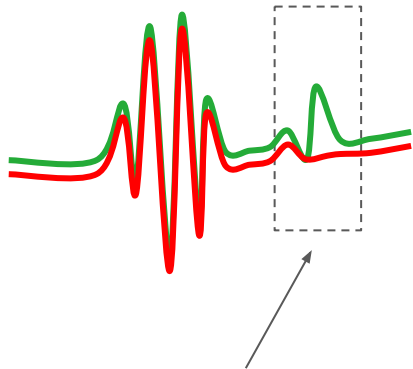
- At node select a random transformation
- At node selects reference histograms per class (exemplars)
- Uses histogram similarity measure
- Partitions the data based on the proximity to reference histograms
- Original BOSS: Uses cross validation
- TS-CHIEF: Uses random transformations



TS-CHIEF : Interval-based splitter

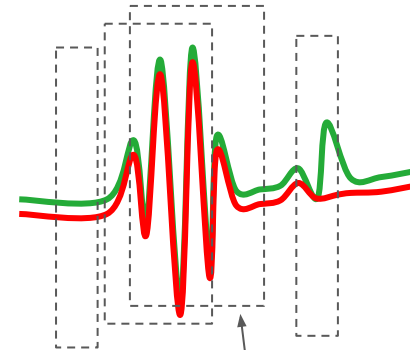
- Select random intervals and transforms
 - time (ACF, PACF, AR) and frequency (PS)
- Attribute-value split similar to classic decision tree

At tree level: RISE



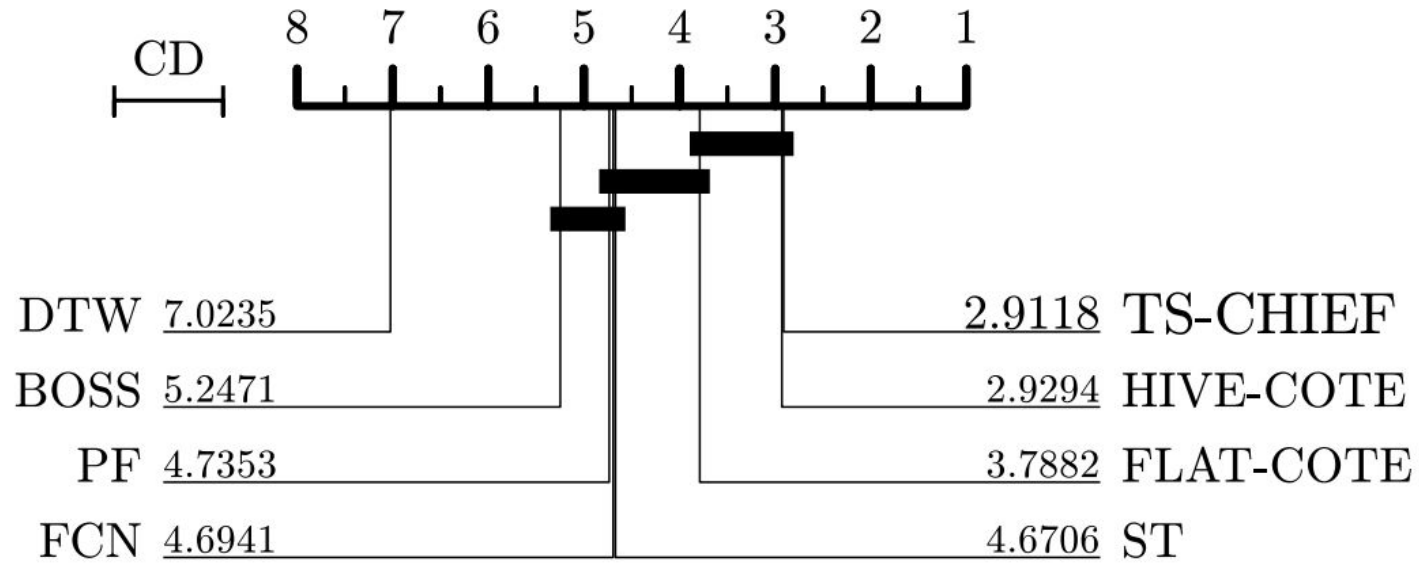
Intervals selected on global discrimination ability

At node level: TS-CHIEF

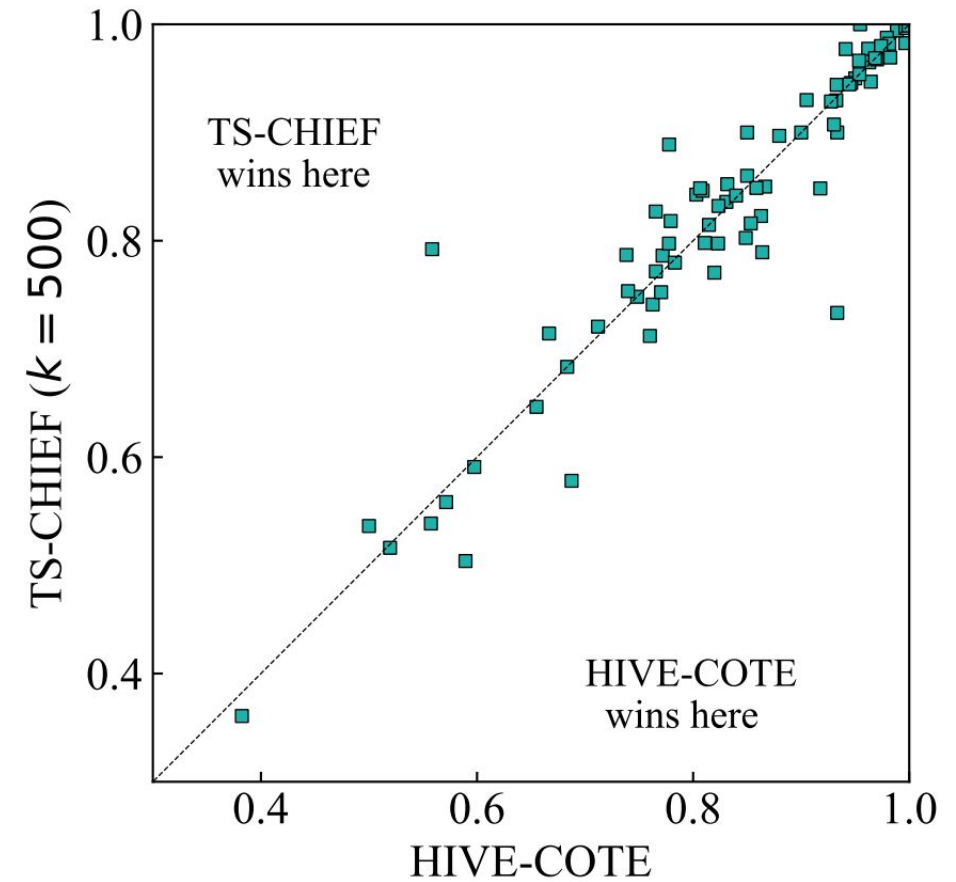
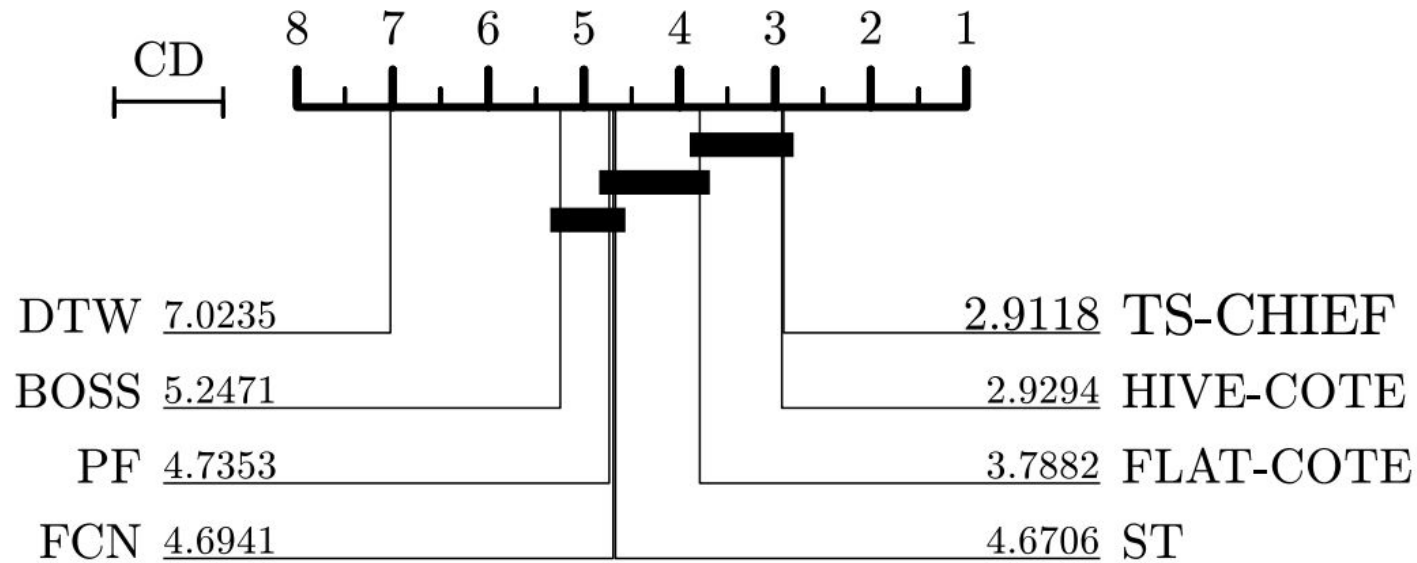


random intervals

Accuracy on 85 UCR datasets



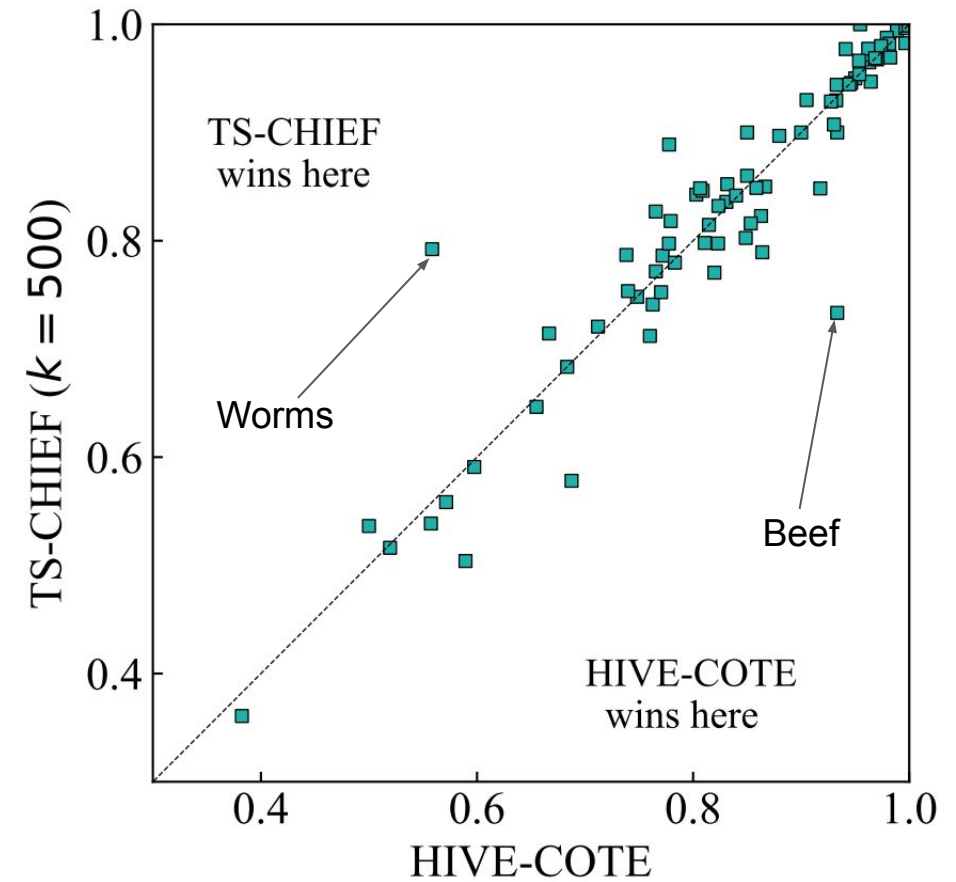
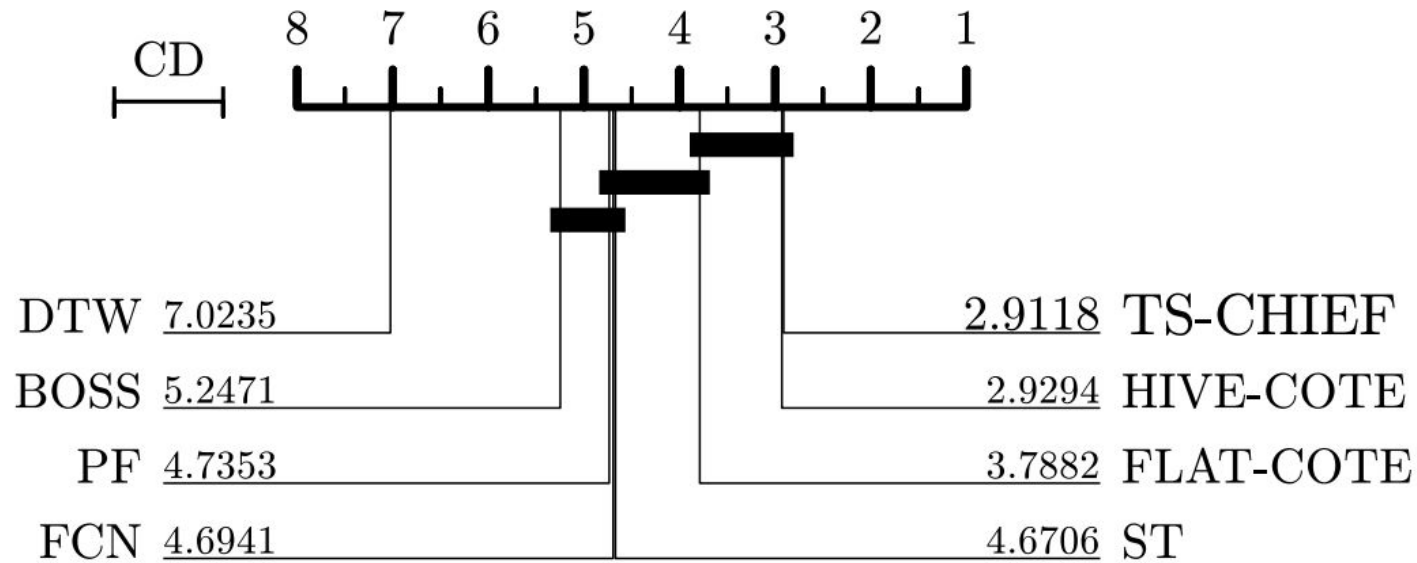
Accuracy on 85 UCR datasets



TS-CHIEF vs HIVE-COTE

41 wins
35 loss
9 ties
 $p=0.42$ (Wilcoxon's test)

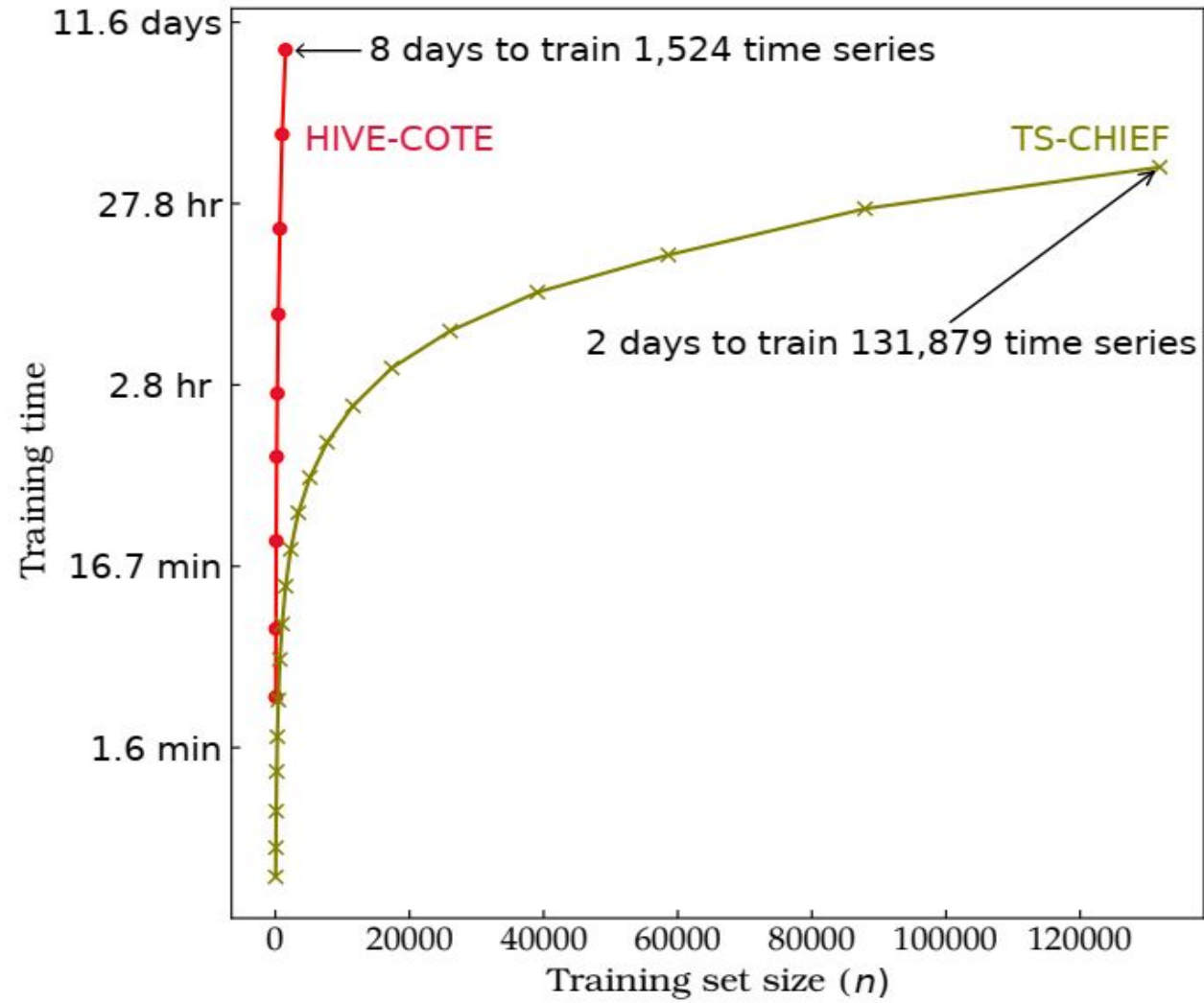
Accuracy on 85 UCR datasets



TS-CHIEF vs HIVE-COTE

41 wins
35 loss
9 ties
 $p=0.42$ (Wilcoxon's test)

Training time vs training size



Training Size

1,500 time series

130,000 time series

HIVE-COTE

8 days

230 years
(estimated)

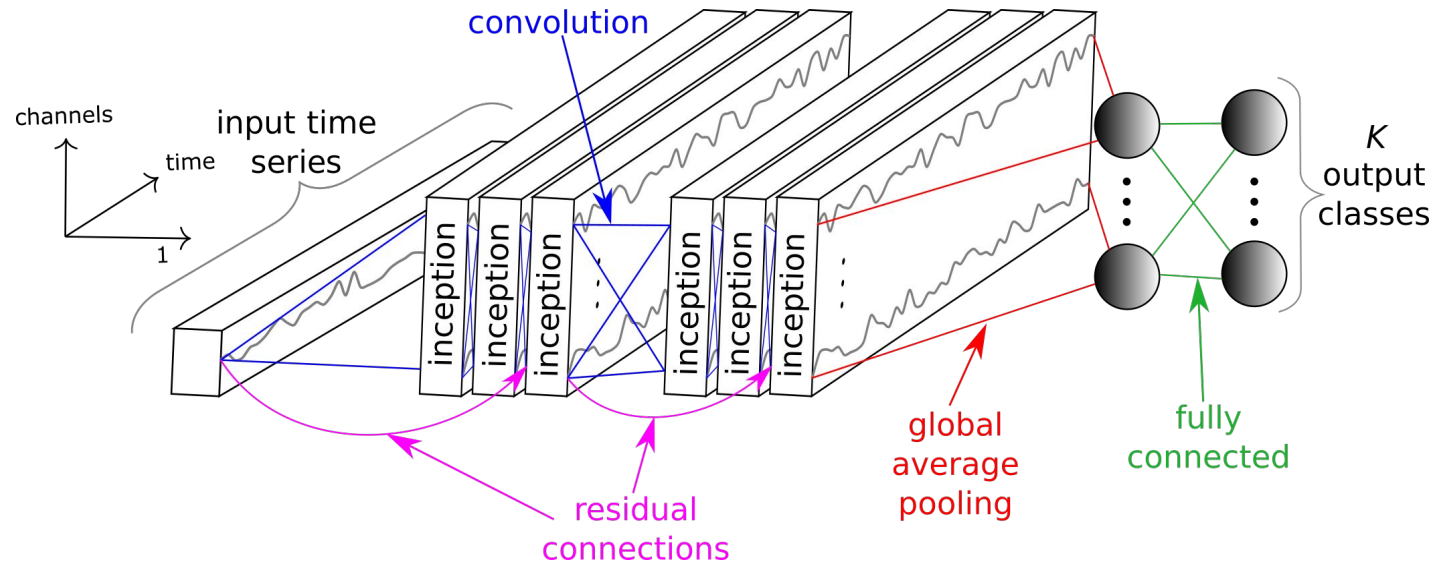
TS-CHIEF

13 min (900x faster)

2 days (46,000x faster)

Part 3: InceptionTime

2019 - arxiv



<http://bit.ly/InceptionTime>

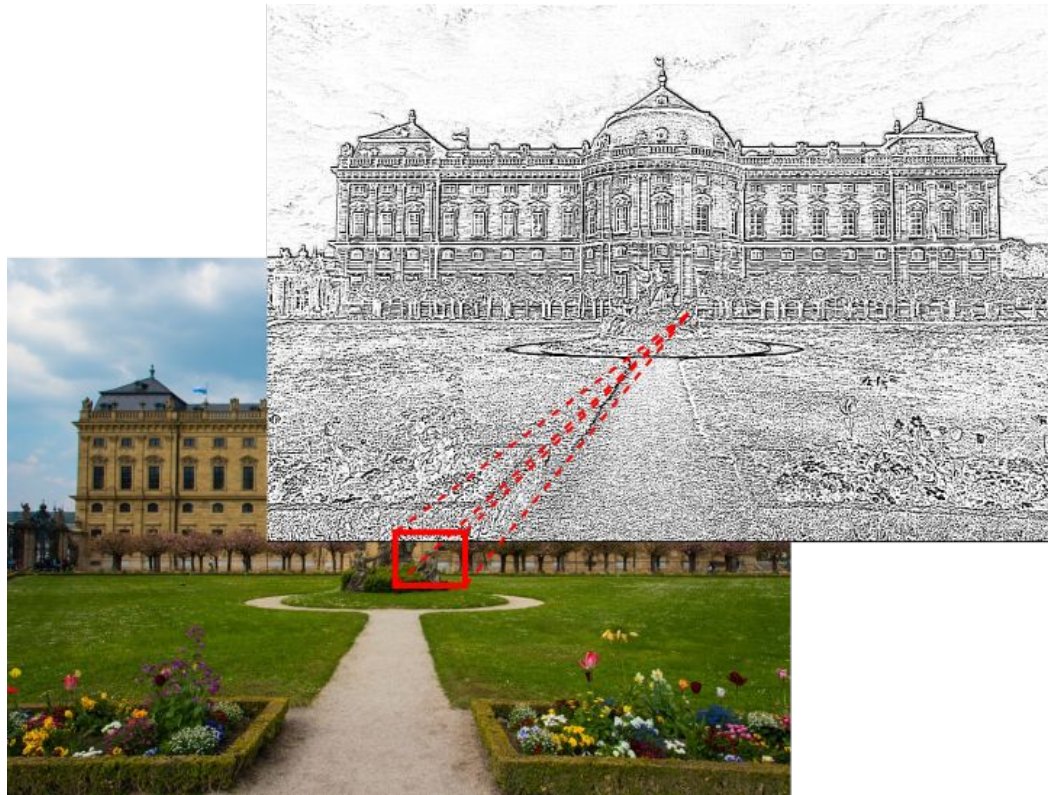
H. Ismail Fawaz, B. Lucas, G. Forestier, C. Pelletier, D. Schmidt, J. Weber, G. Webb, L. Idoumghar, P-A. Muller, F. Petitjean (2019). InceptionTime: Finding AlexNet for Time Series Classification. *under review*. <https://arxiv.org/abs/1909.04939>

Deep Learning

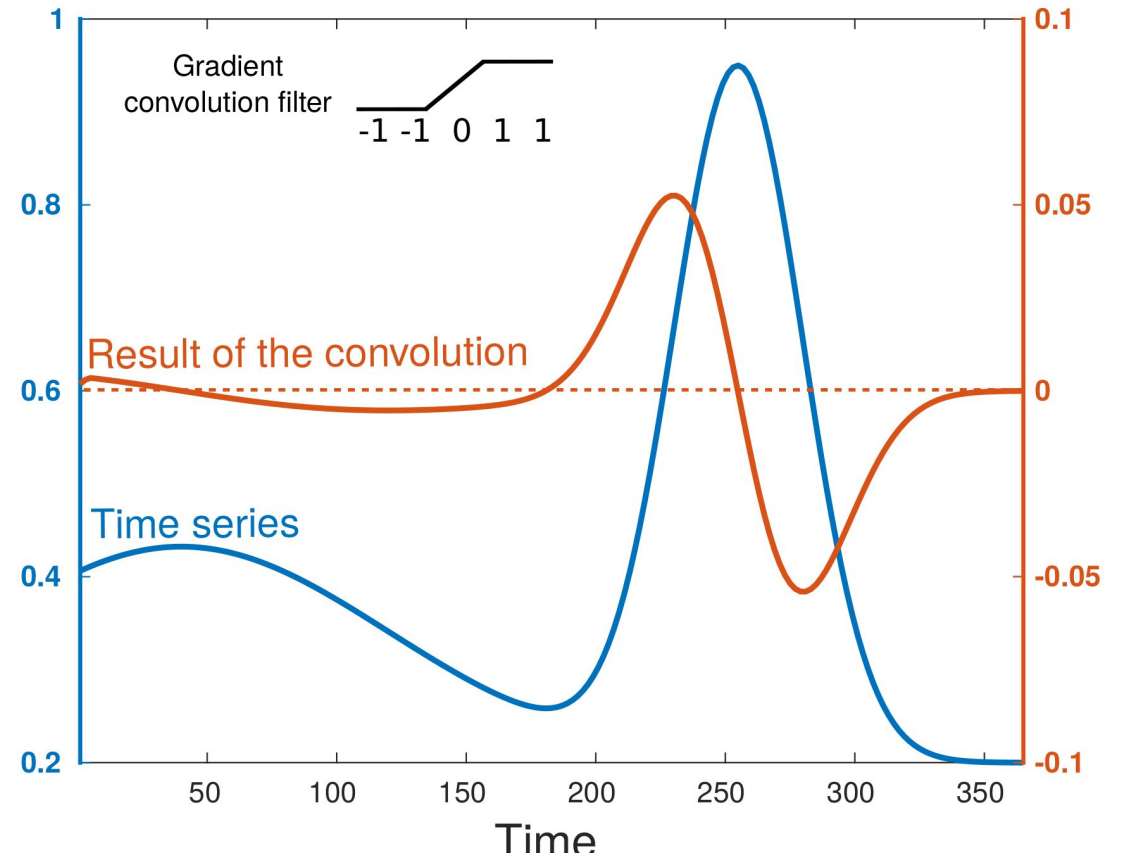
- Revolutionized the field of computer vision [1]
- Reached human level performance in image recognition tasks [2]
- Adopted by the Natural Language Processing (NLP) community [3]
- Improved state of the art speech recognition systems[4]

1. Krizhevsky, A., Sutskever, I., & Hinton, G. E. (2012). Imagenet classification with deep convolutional neural networks. In Advances in Neural Information Processing Systems
2. Szegedy, C., Liu, W., Jia, Y., Sermanet, P., Reed, S., Anguelov, D., et al. (2015). Going deeper with convolutions. In Proceedings of IEEE Conference on Computer Vision and Pattern Recognition
3. Young, T., Hazarika, D., Poria, S., & Cambria, E. (2018). Recent trends in deep learning based natural language processing. IEEE Computational intelligence magazine, 13(3), 55-75.
4. Hinton, G., Deng, L., Yu, D., Dahl, G. E., Mohamed, A. R., Jaitly, N., et al. (2012). Deep neural networks for acoustic modeling in speech recognition: The shared views of four research groups. IEEE Signal Processing Magazine

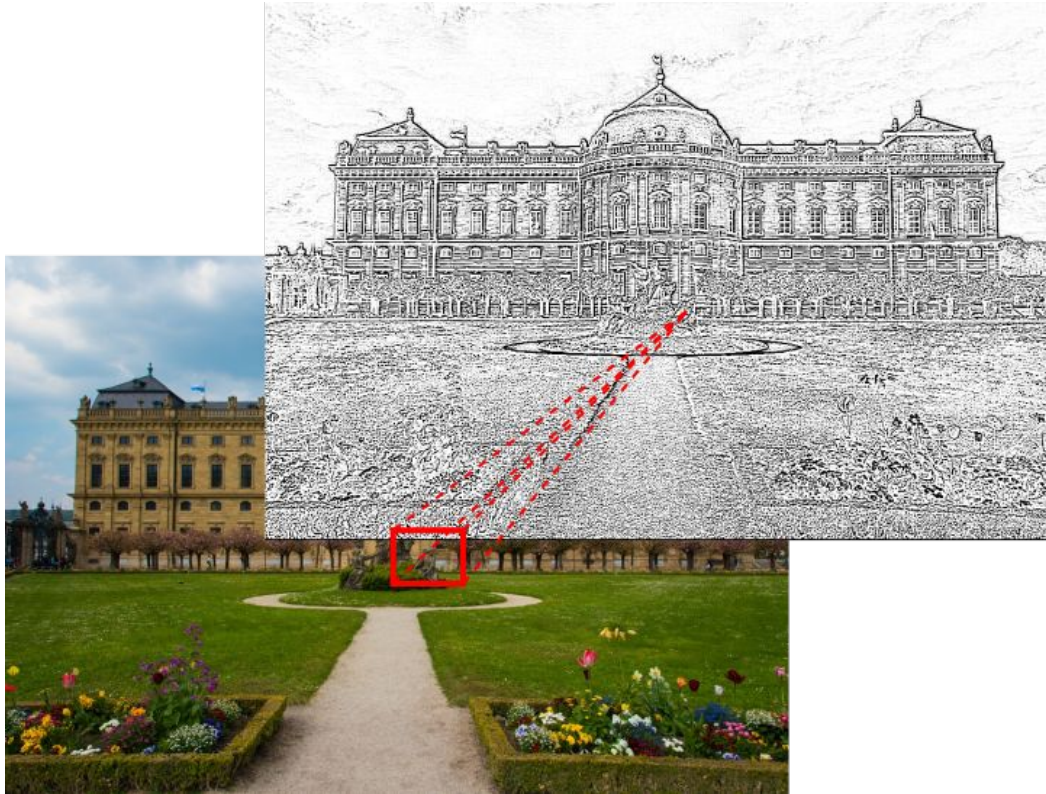
Convolution on images vs. time series



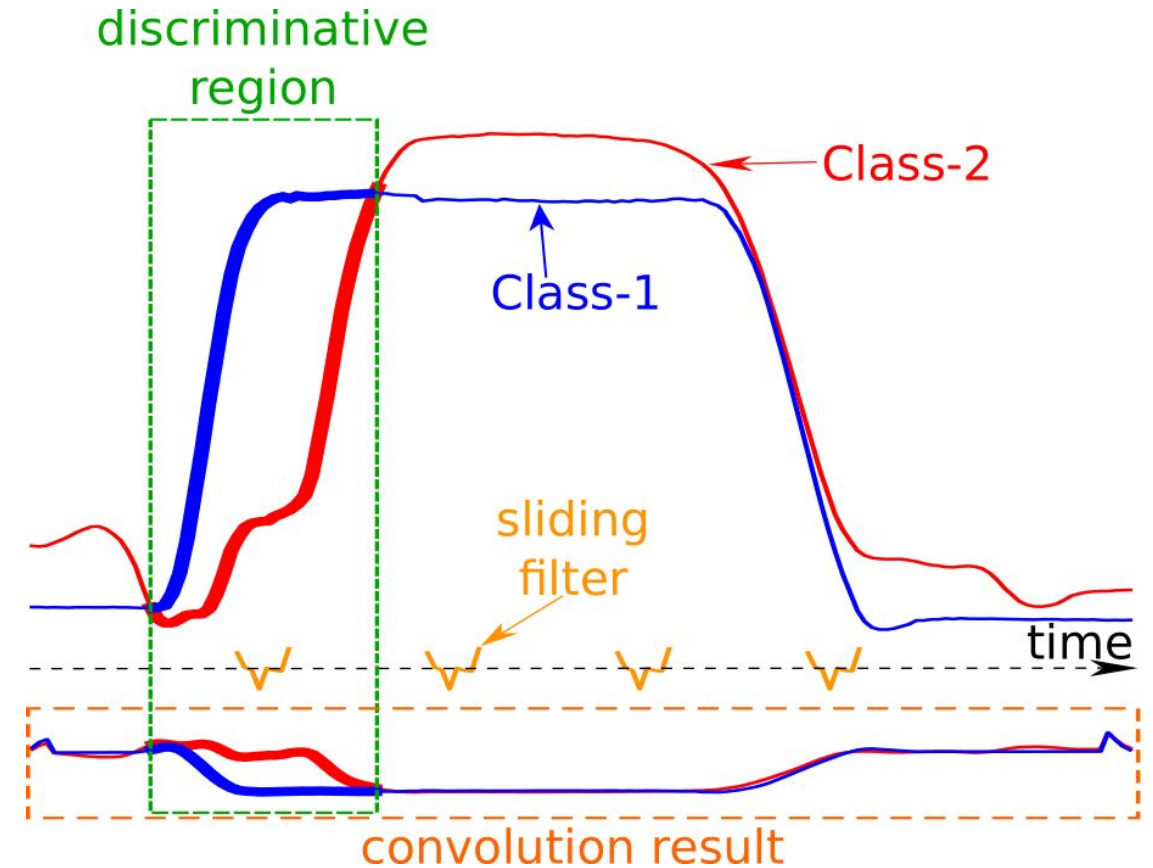
The result of applying an edge detection convolution on an image



Convolution on images vs. time series

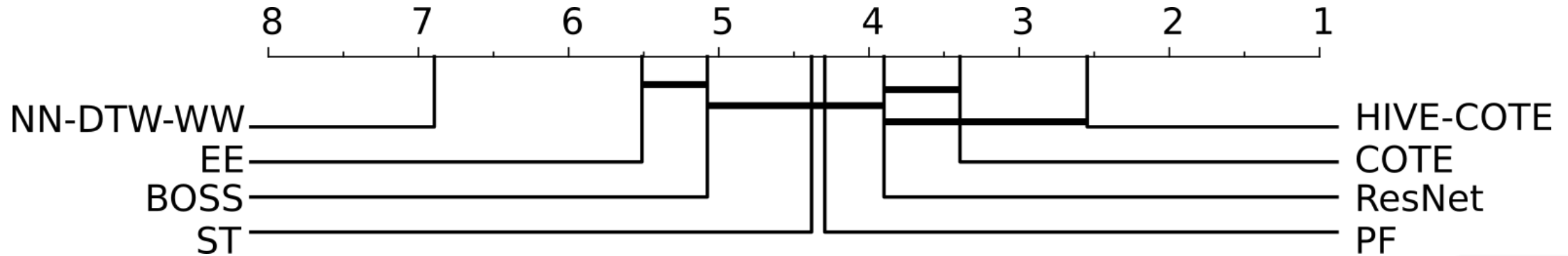


The result of applying an edge detection convolution on an image



The result of applying a learned discriminative convolution on the GunPoint dataset

Deep learning for Time Series Classification



A critical difference diagram showing how ResNet still lacks behind the state of the art classifiers [1]

- Residual Network (ResNet) was originally proposed in [2]
- Currently is the state-of-the-art deep learning model for TSC [1]
- Designed to be a "baseline architecture" for TSC

1. Ismail Fawaz, H., Forestier, G., Weber, J., Idoumghar, L., & Muller, P. A. (2019). Deep learning for time series classification: a review. *Data Mining and Knowledge Discovery*, 33(4), 917-963.
2. Wang, Z., Yan, W., & Oates, T. (2017, May). Time series classification from scratch with deep neural networks: A strong baseline. In *IEEE International Joint Conference on Neural Networks*.

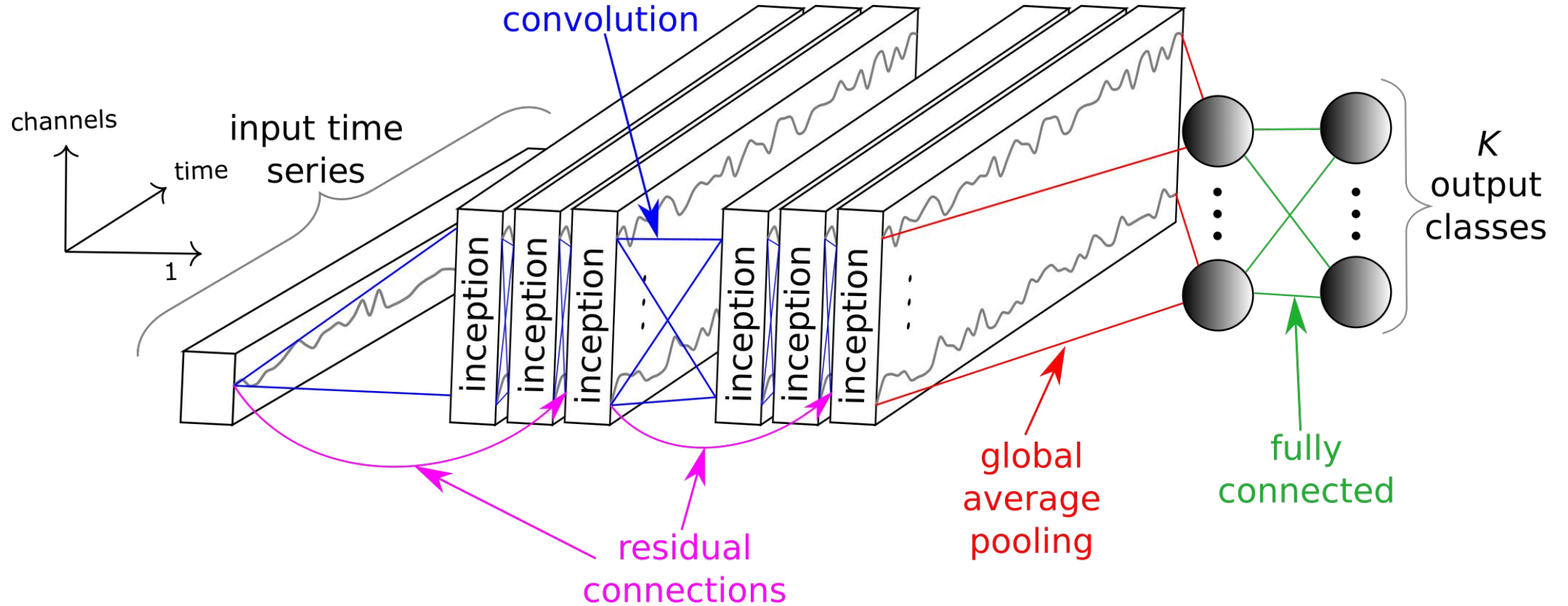


Inception

- Originally proposed by Google for image recognition problems [1]
- Further developed to reach state-of-the-art results on ImageNet [2]
- Main idea:
 - Apply convolutions of different resolutions to capture different patterns
 - Use a bottleneck layer in order to reduce the number of parameters
- For TSC, Inception had not been yet explored

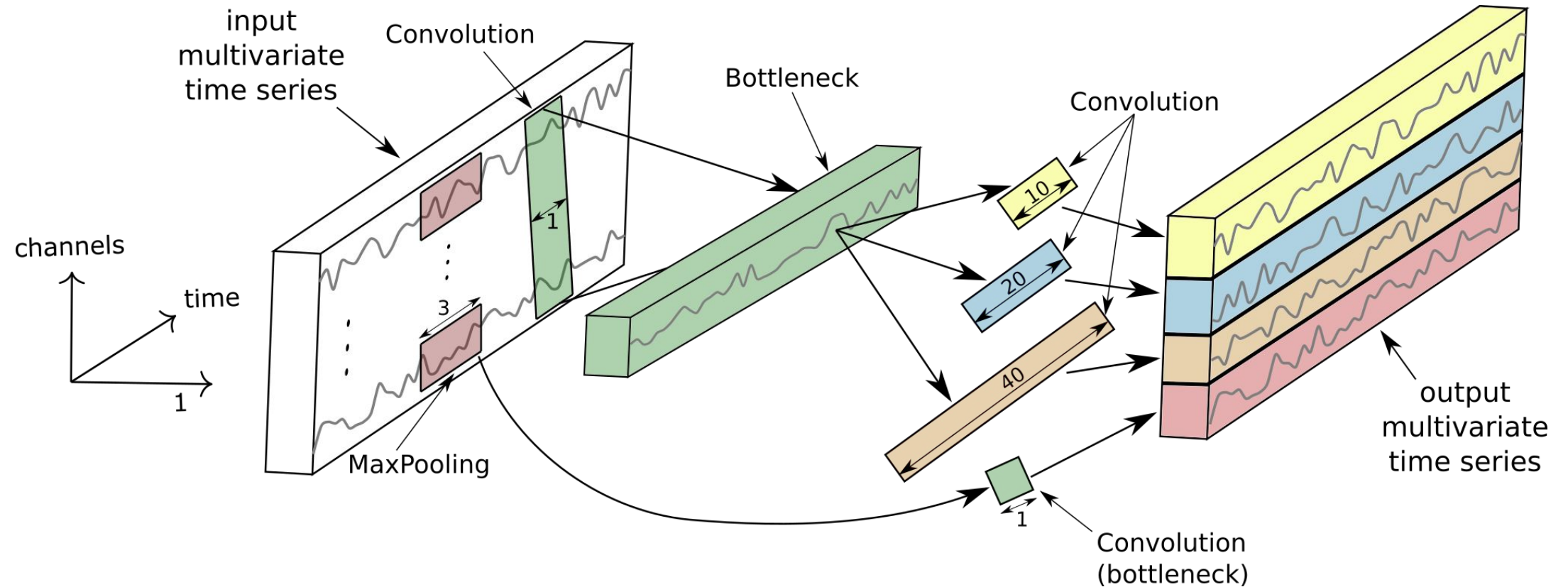
1. Szegedy, C., Liu, W., Jia, Y., Sermanet, P., Reed, S., Anguelov, D., Erhan, D., Vanhoucke, V., & Rabinovich, A. (2015). Going deeper with convolutions. In Proceedings of the IEEE conference on computer vision and pattern recognition (pp. 1-9).
2. Szegedy, C., Vanhoucke, V., Ioffe, S., Shlens, J., & Wojna, Z. (2016). Rethinking the inception architecture for computer vision. In *Proceedings of the IEEE conference on computer vision and pattern recognition* (pp. 2818-2826).

Our InceptionTime architecture for TSC



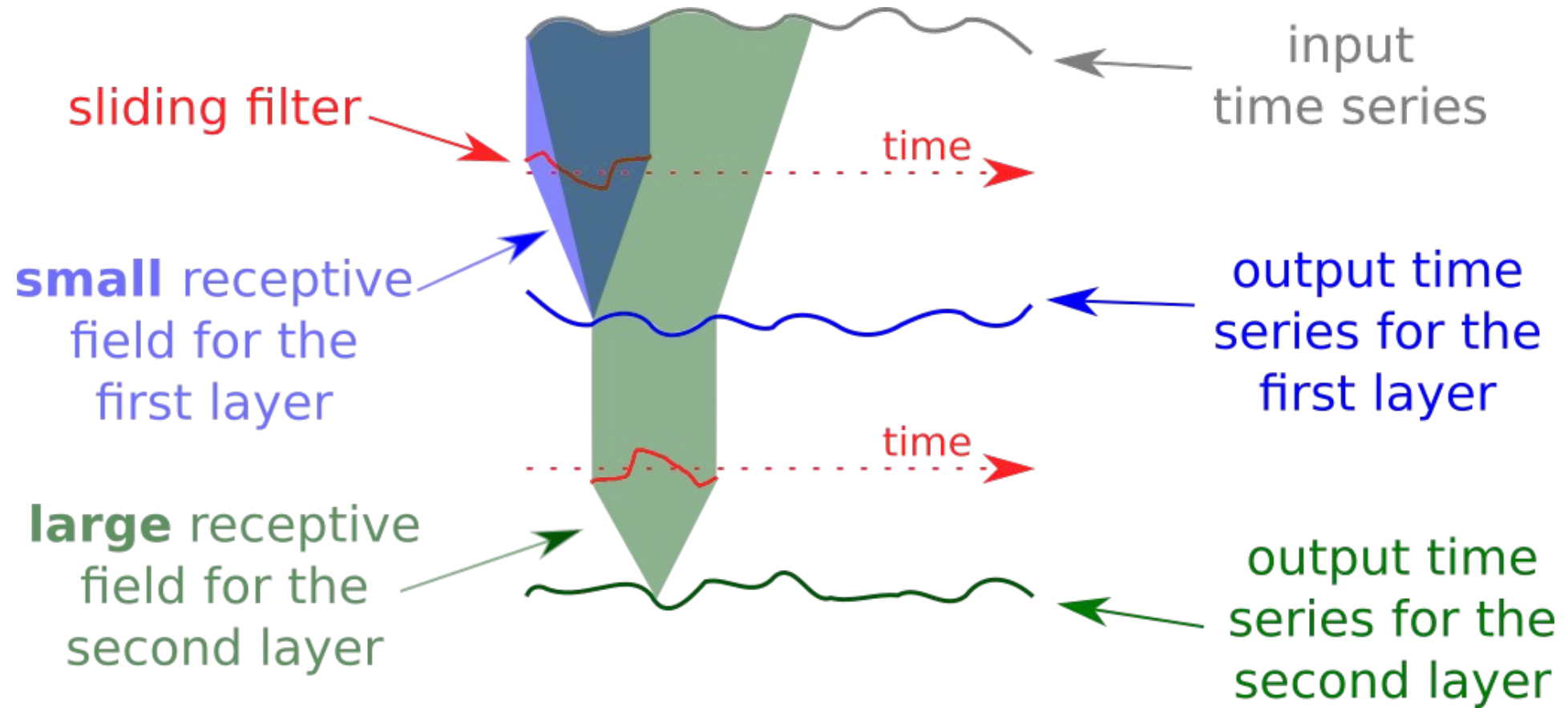
Inception network for time series classification

Inception module for time series classification



Inside our Inception module for time series classification

Receptive Field (RF) of a neural network



Receptive field illustration for a two layers CNN

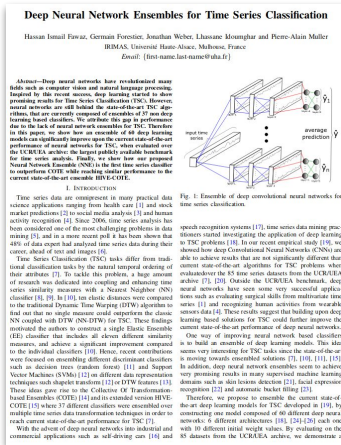
InceptionTime: an ensemble of 5 networks

$$\hat{y}_{i,c} = \frac{1}{n} \sum_{j=1}^n \sigma_c(x_i, \theta_j) \quad | \quad \forall c \in [1, C]$$

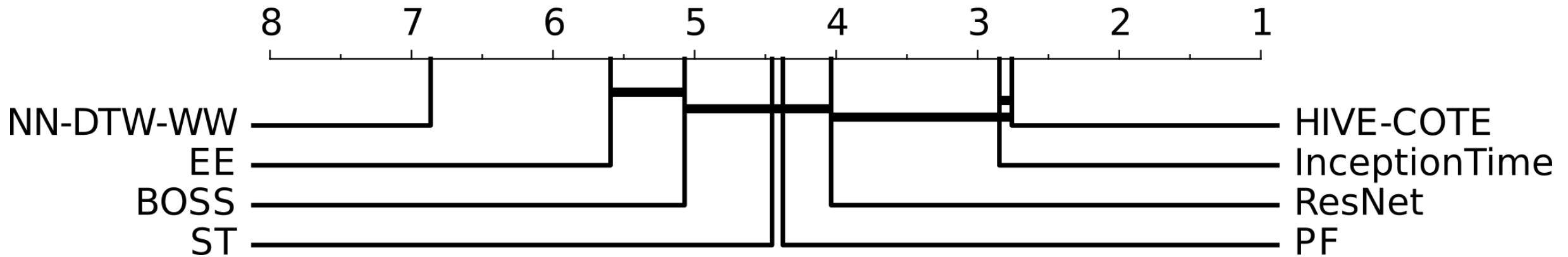
- Ensembling deep nets for TSC studied by Hassan in [1]
- Bias/variance tells us that this works because different initializations lead to very different networks (low covariance)

$$\text{MSE}(H) = \overline{\text{bias}(H)}^2 + \frac{1}{|H|} \overline{\text{variance}(H)} + \left(1 - \frac{1}{|H|}\right) \overline{\text{covariance}(H)}$$

1. Ismail Fawaz, H., Forestier, G., Weber, J., Idoumghar, L., & Muller, P. (2019). Deep neural network ensembles for time series classification. IEEE International Joint Conference on Neural Networks.



Accuracy results on the UCR archive



Critical difference diagram showing the performance of InceptionTime compared to the current state-of-the-art classifiers of time series data

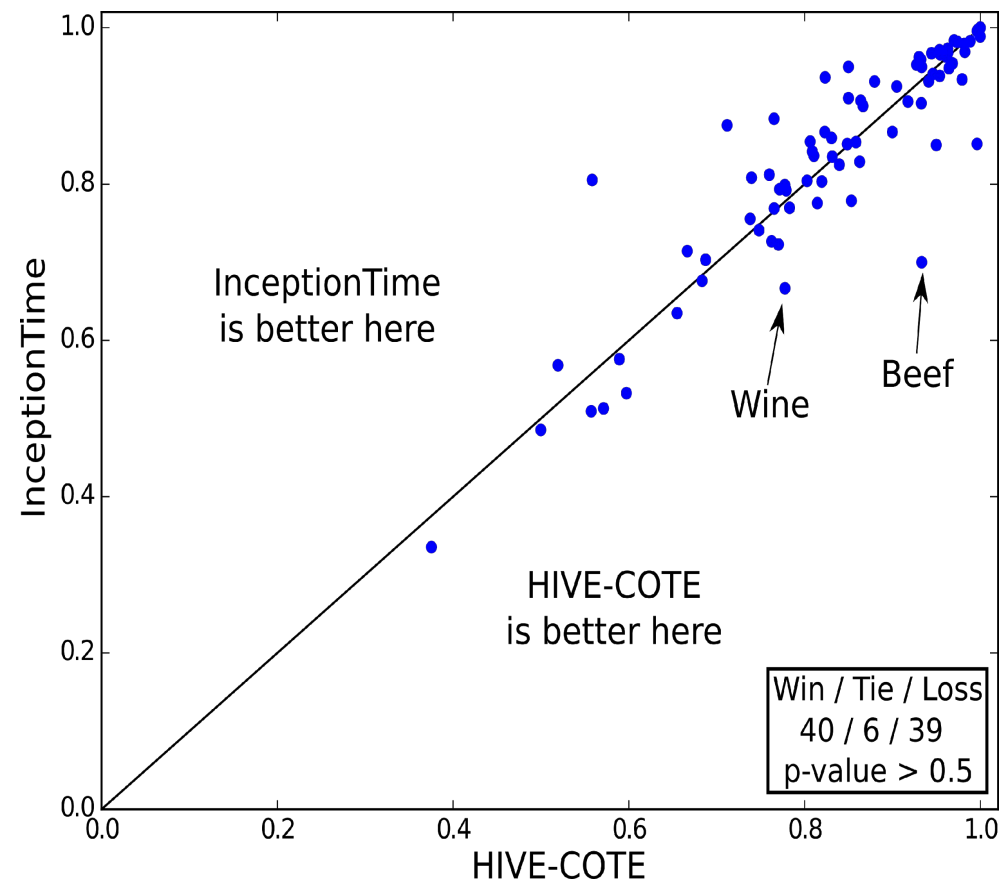
- InceptionTime reaches very similar results to HIVE-COTE

Bagnall, A., Lines, J., Bostrom, A., Large, J., & Keogh, E. (2017). The great time series classification bake off: a review and experimental evaluation of recent algorithmic advances. *Data Mining and Knowledge Discovery*, 31(3), 606-660.

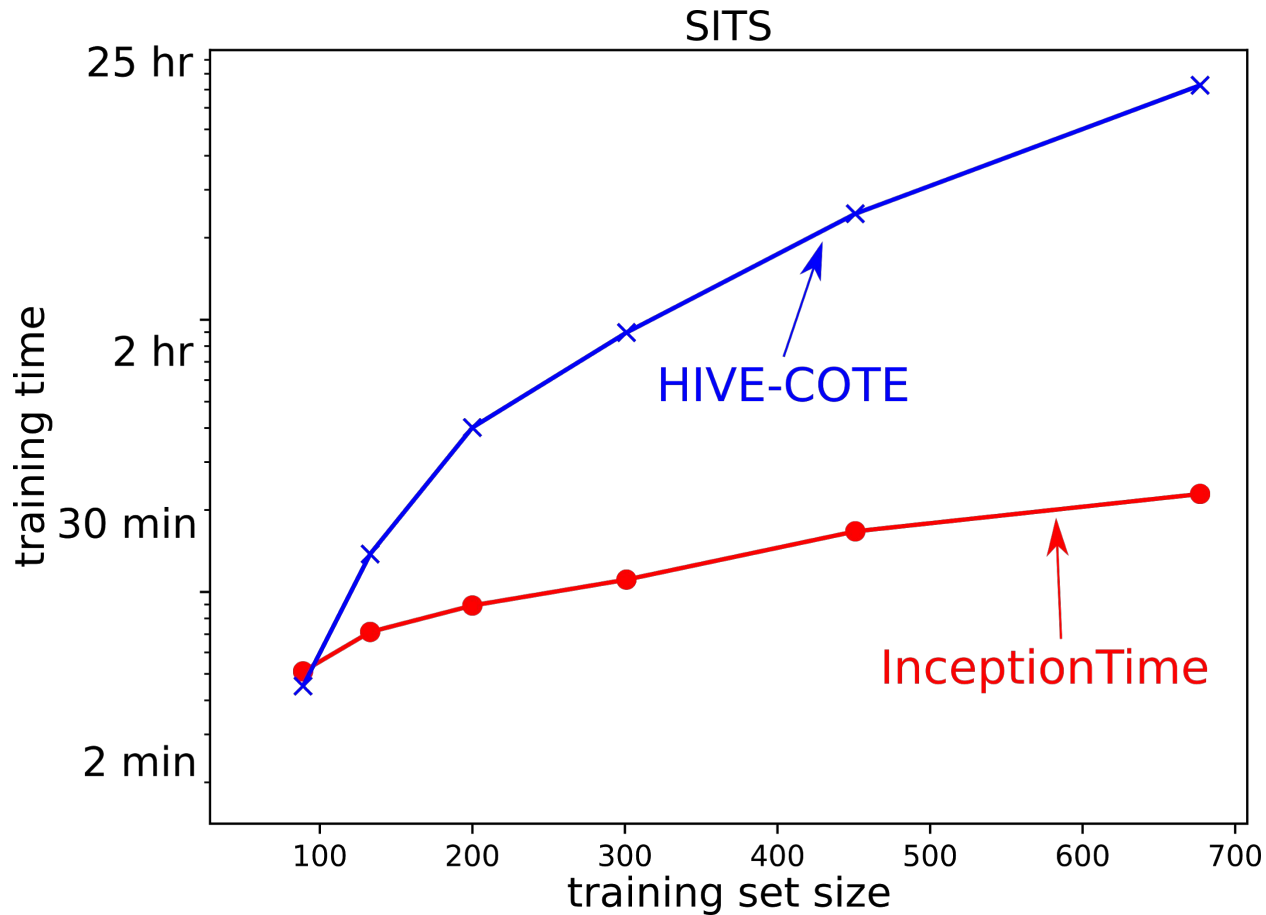
Accuracy plot: InceptionTime vs HIVE-COTE

- InceptionTime is slightly better than HIVE-COTE on average [1]
- Wine and Beef were shown to benefit from transfer learning [2]

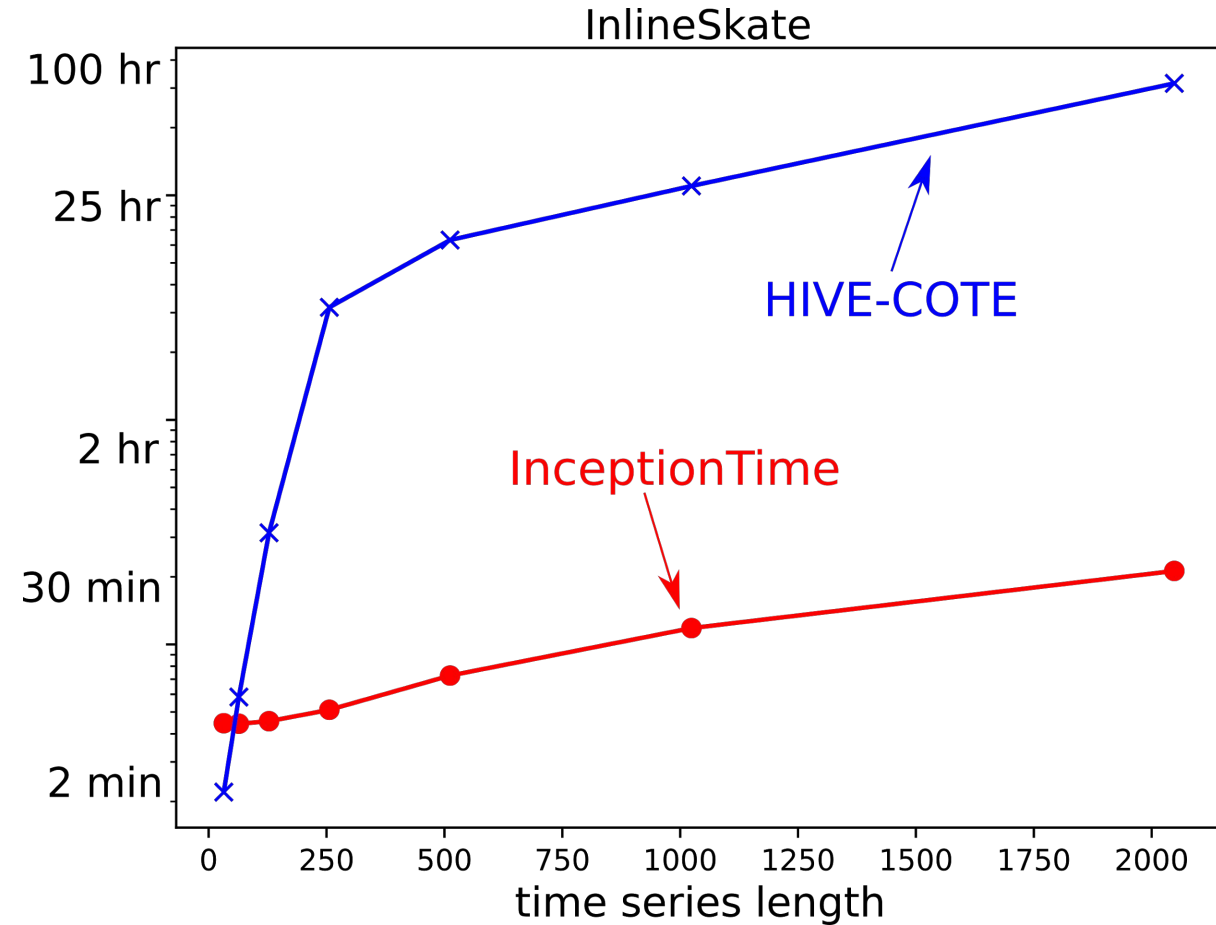
1. Lines, J., Taylor, S., & Bagnall, A. (2018). Time series classification with HIVE-COTE: The hierarchical vote collective of transformation-based ensembles. *ACM Transactions on Knowledge Discovery from Data (TKDD)*, 12(5), 52.
2. Ismail Fawaz, H. I., Forestier, G., Weber, J., Idoumghar, L., & Muller, P. A. (2018). Transfer learning for time series classification. In IEEE International Conference on Big Data.



Training time comparison with HIVE-COTE

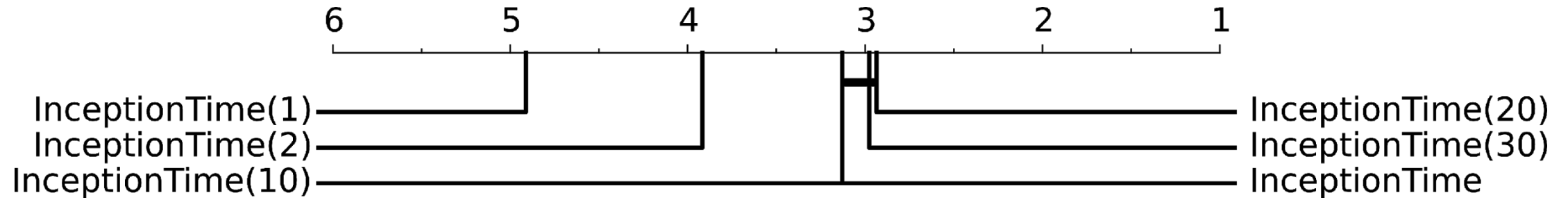


Training time as a function of the training set size for the SITS dataset



Training time as a function of the series length for the InlineSkate dataset

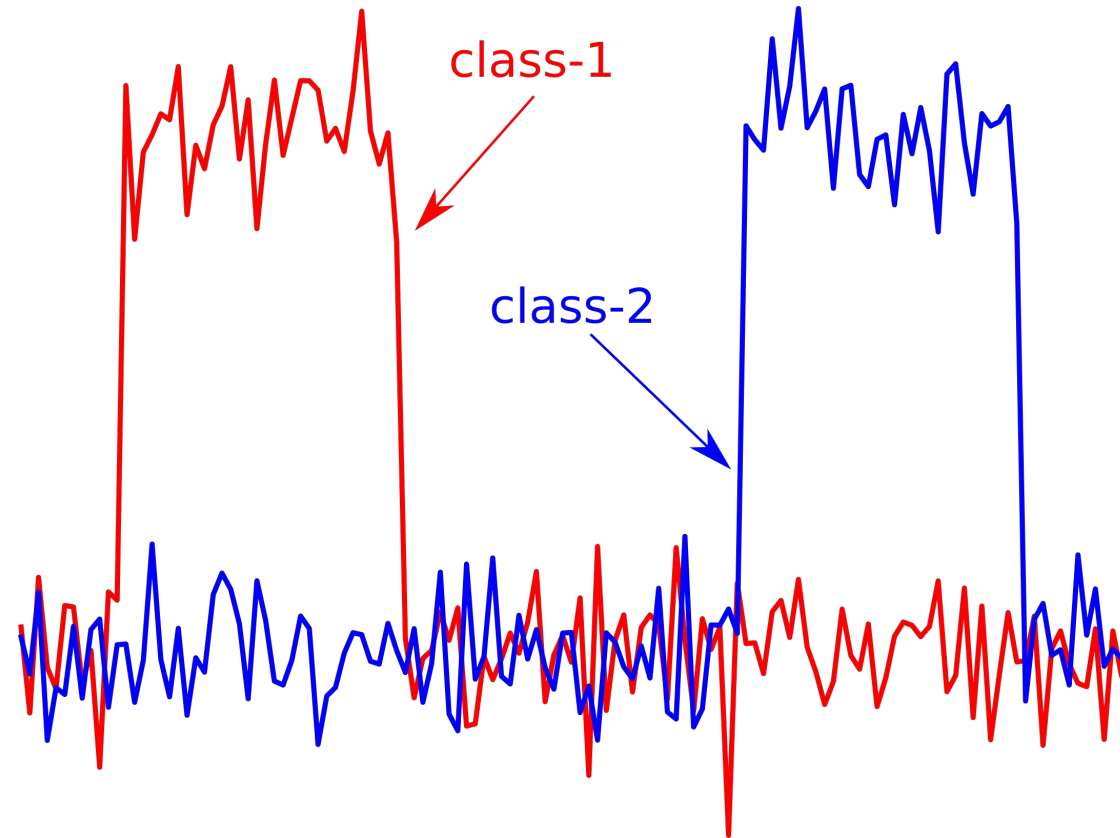
Studying the size of the ensemble



Critical difference diagram showing the effect of the number of individual classifiers in InceptionTime

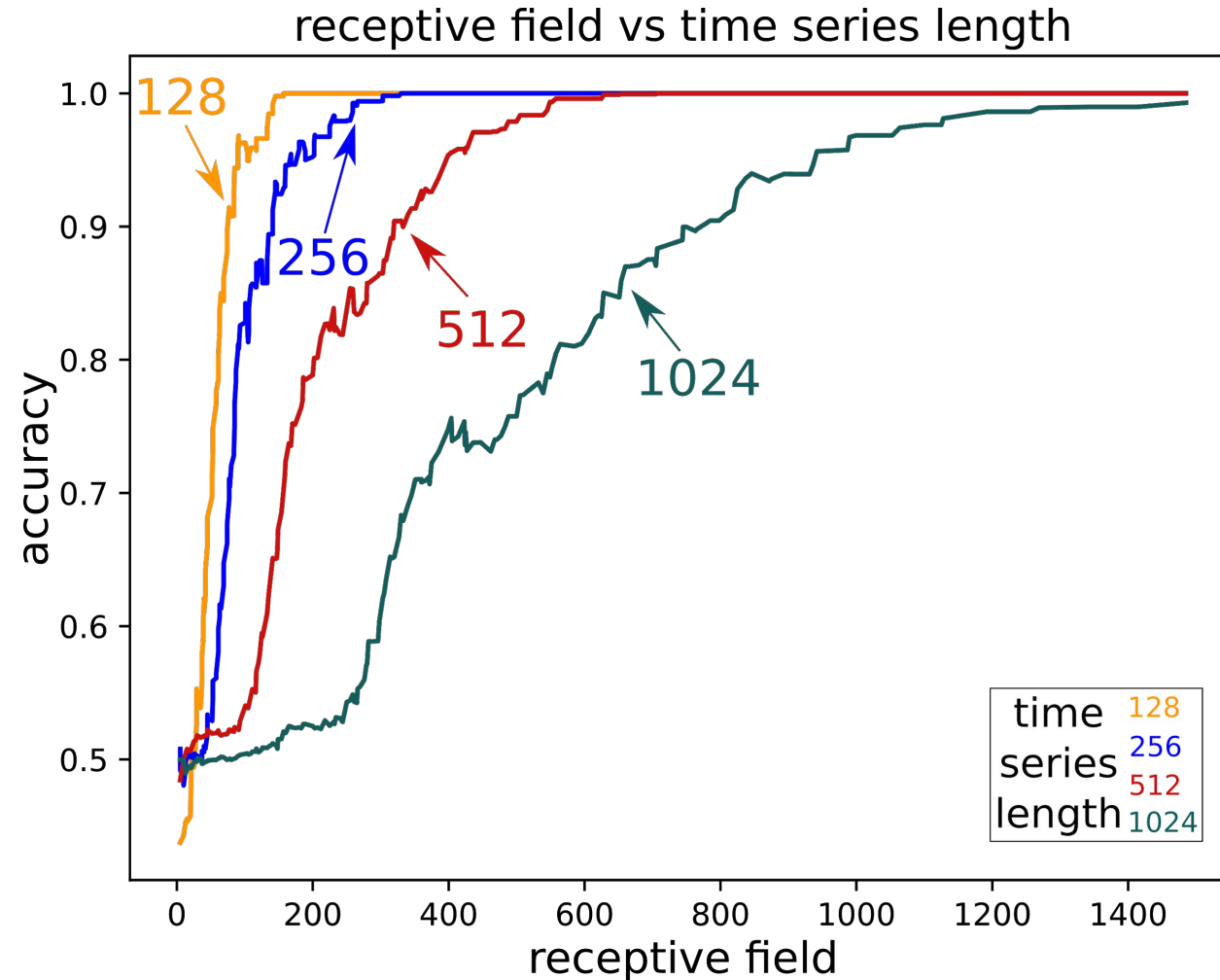
- InceptionTime(x) denotes an ensemble of x Inception networks
- InceptionTime is equivalent to InceptionTime(5)
- There is no significant improvement for $x \geq 5$
 - Again this is due to covariance that start hurting us from 5 elements
 - Therefore we decided to stick with InceptionTime(5)

Hyperparameter study: synthetic dataset



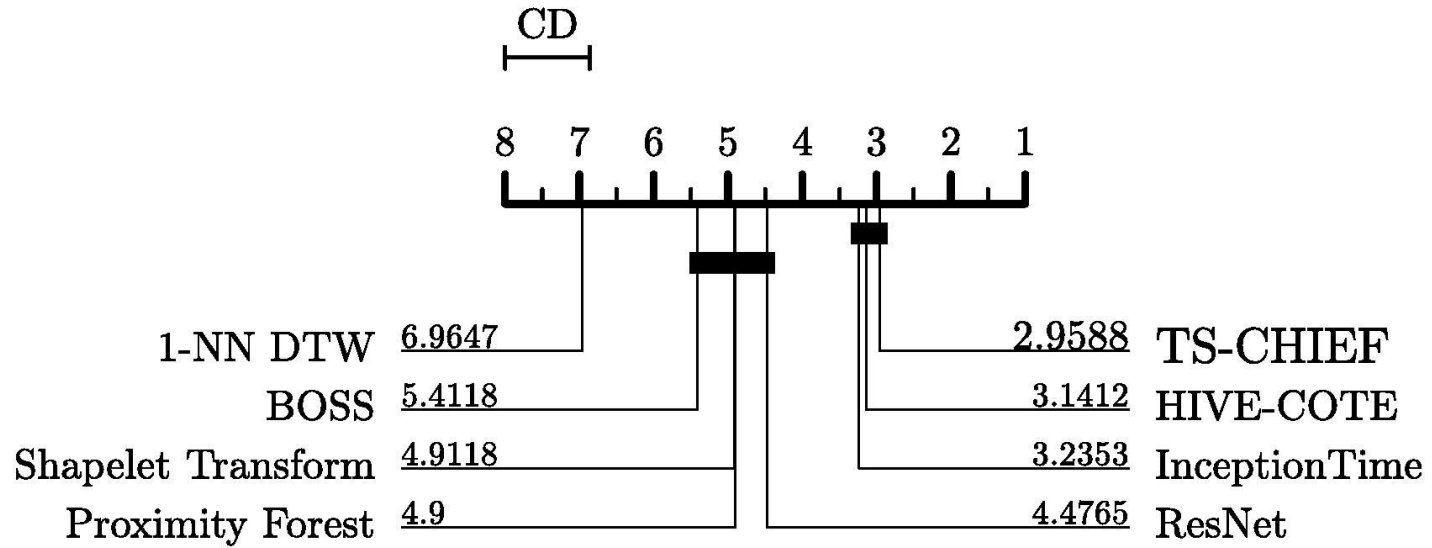
Example of a synthetic binary time series classification problem

Hyperparameter study: Receptive Field (RF)

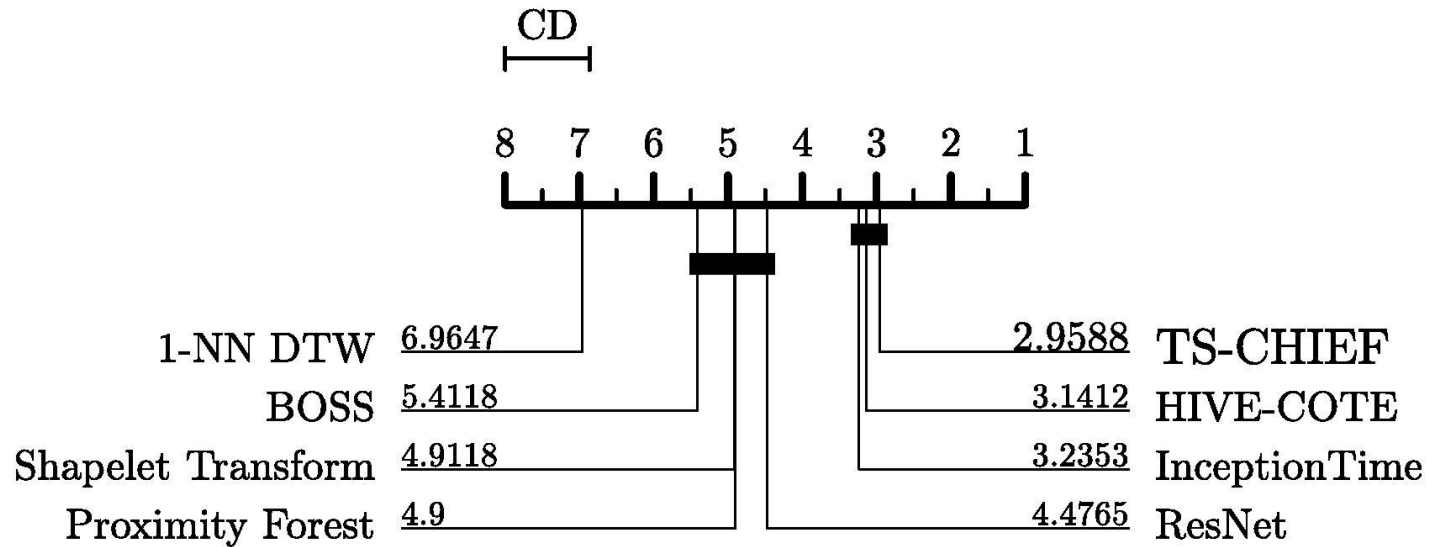


A larger receptive field is needed to classify very long time series

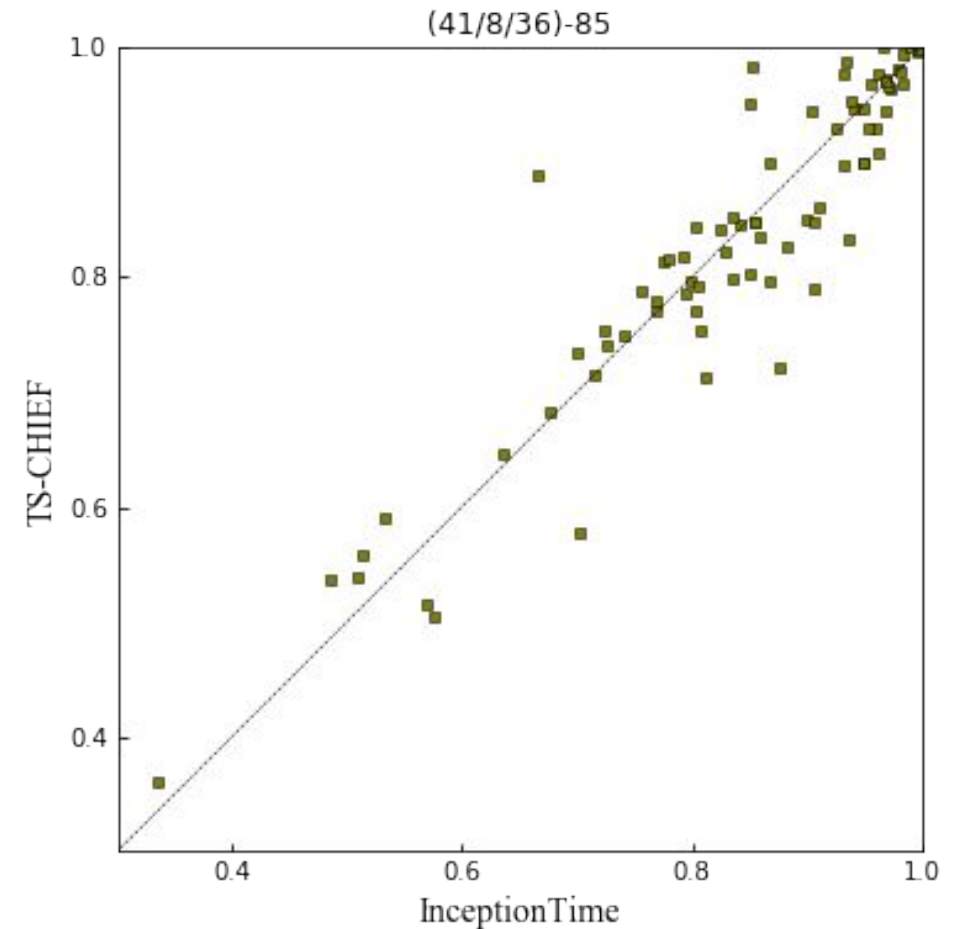
TS-CHIEF vs InceptionTime



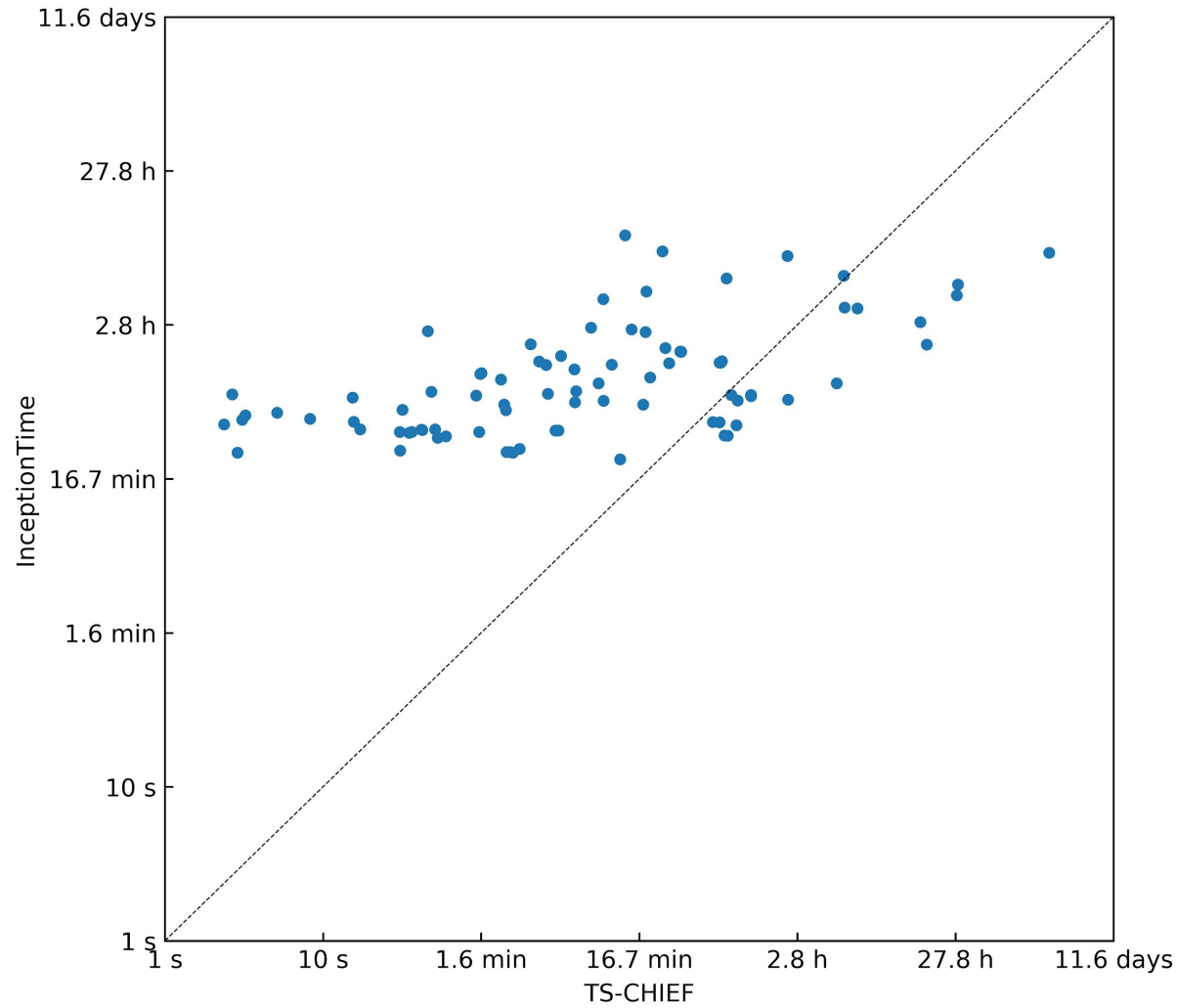
TS-CHIEF vs InceptionTime



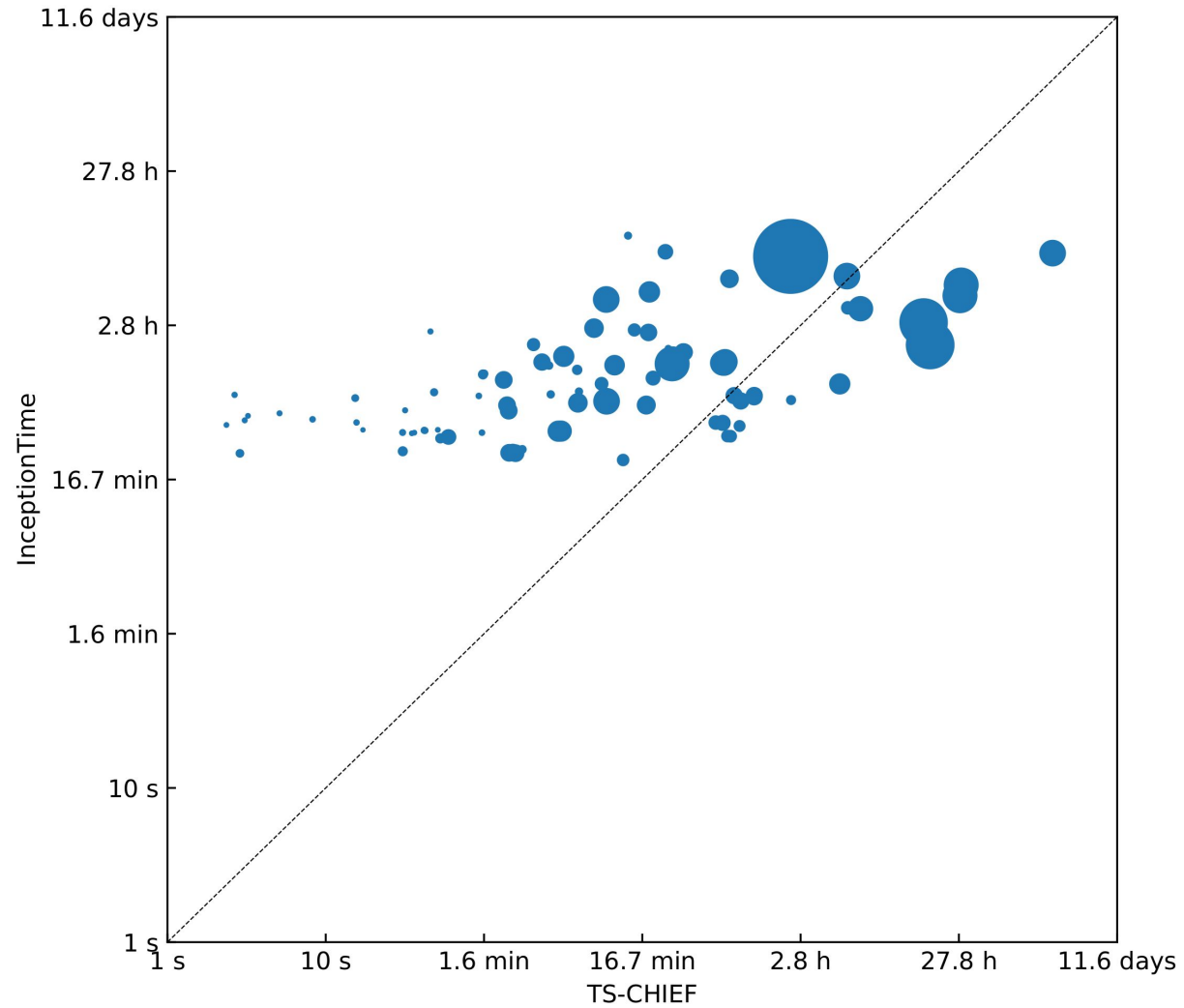
- TS-CHIEF wins on average in terms of WDL
- But, lots of big wins with InceptionTime



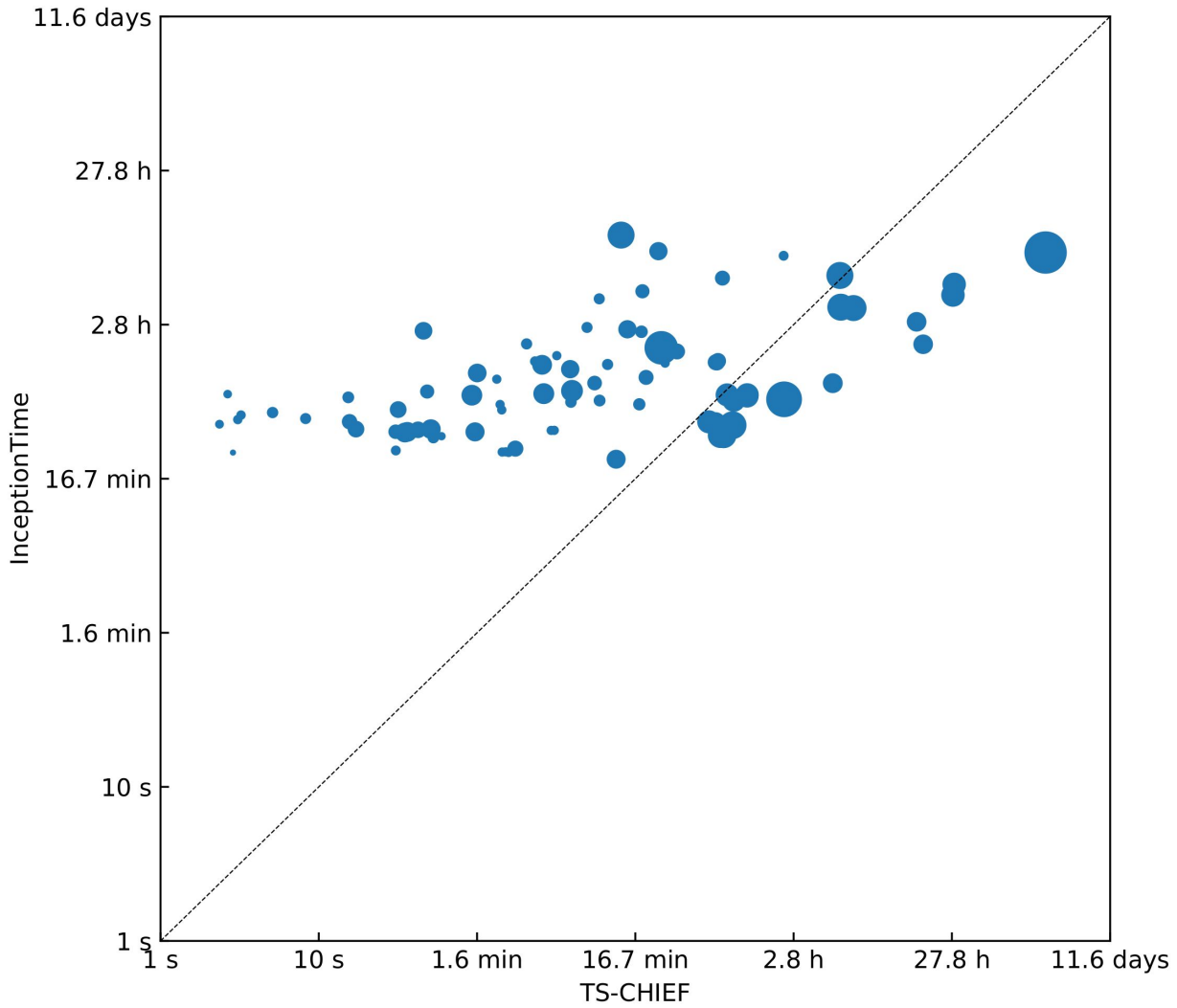
TS-CHIEF vs InceptionTime - training time



TS-CHIEF vs InceptionTime - training time

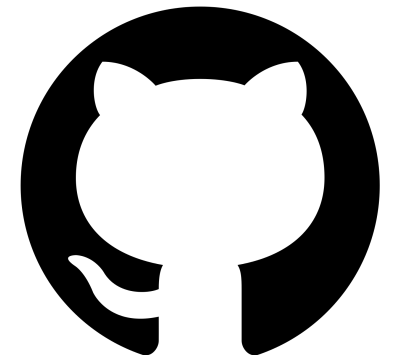


TS-CHIEF vs InceptionTime - training time



Conclusions

- Ensemble techniques have revolutionised time series classification with Tony and Jason's group giving us a beacon for research
- TS-Chief combines the efficiencies of tree-based divide-and-conquer with random split selection and the effectiveness of decades' worth of specialised time series techniques
- InceptionTime brings the power and efficiency of deep learning
- Both make state-of-the-art accuracy computationally feasible for large learning tasks
- We believe in reproducible research:
 - Proximity Forest → <https://github.com/fpetitjean/ProximityForest>
 - TS-CHIEF → <https://github.com/dotnet54/TS-CHIEF>
 - InceptionTime → <https://github.com/hfawaz/InceptionTime>





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Thank you!

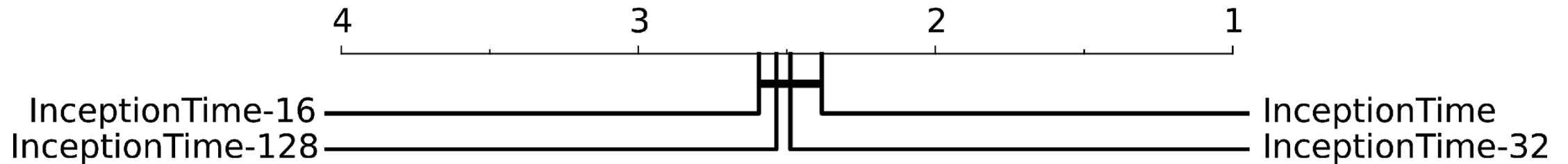


<http://francois-petitjean.com>



Additional slides

Hyperparameter study: batch size



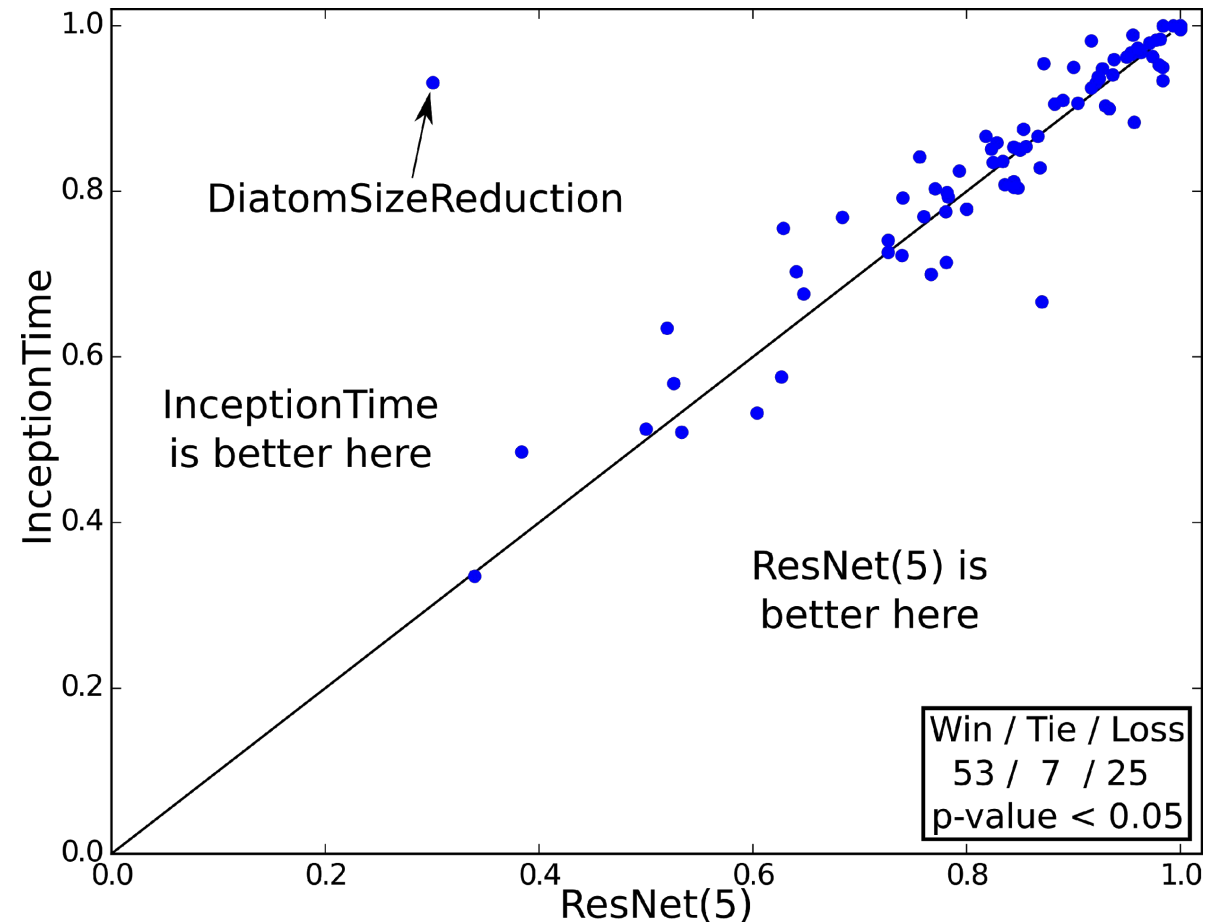
Critical difference diagram showing the effect of the batch size hyperparameter value over InceptionTime's average rank

- InceptionTime- x denotes InceptionTime with a batch size equal to x
- InceptionTime is equivalent to InceptionTime-64 (default value)
- There is no significant difference between the different models
- A value equal to 64 shows a small non-significant superiority
- We therefore chose to stick with a batch size equal to 64

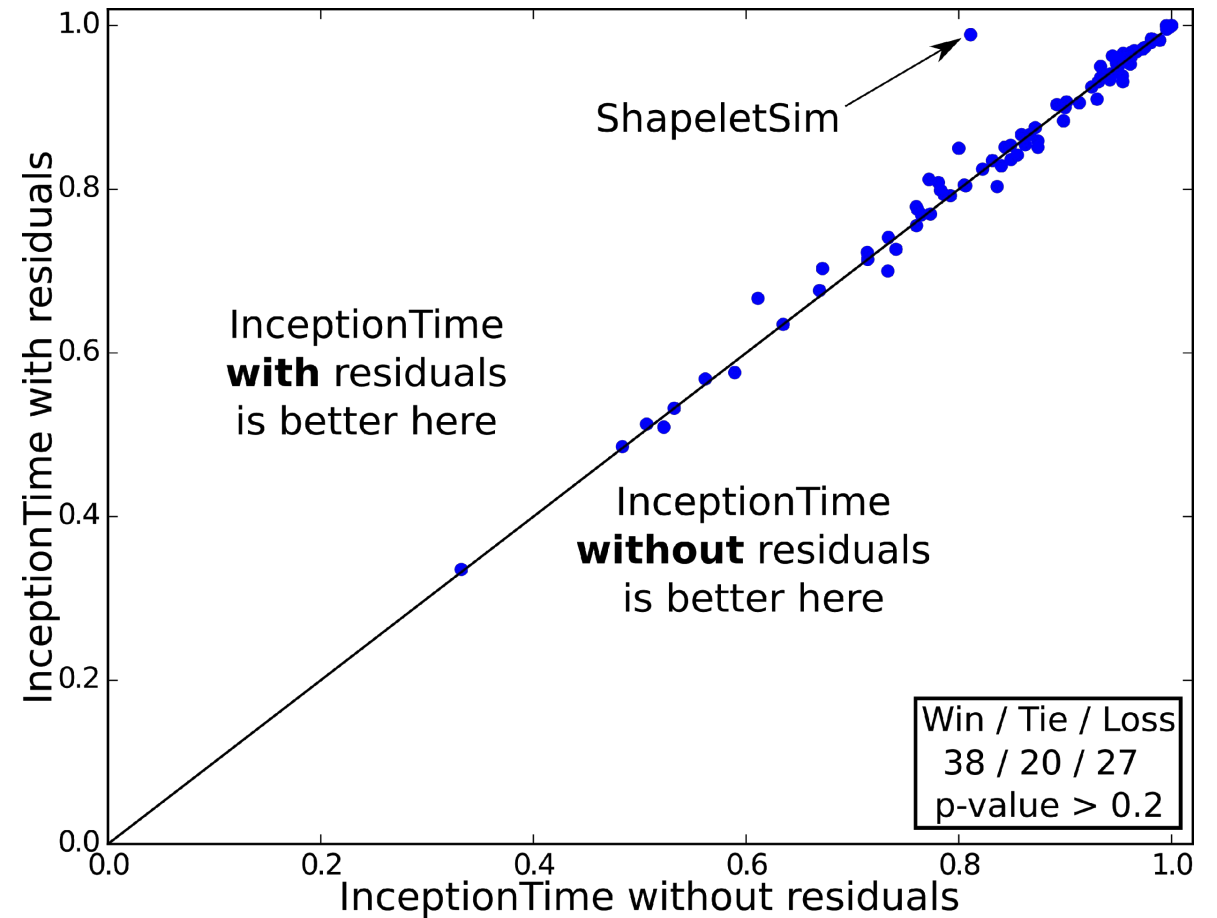
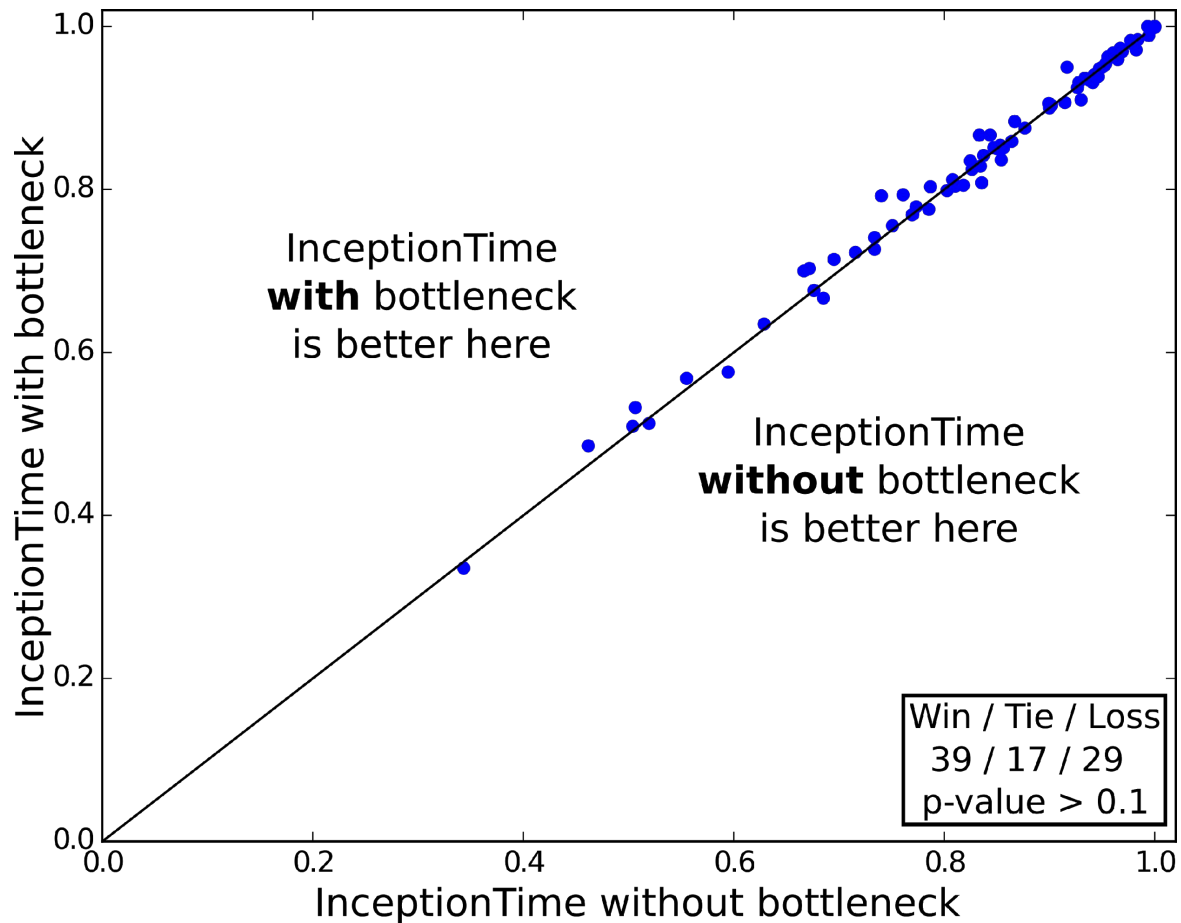
Accuracy plot: InceptionTime vs ResNet(5)

- InceptionTime significantly outperforms ResNet(5) [1]
- For DiatomSizeReduction the main improvement is from using a batch size larger than 1 (which is the case for the ResNet model for this specific dataset)

1. Ismail Fawaz, H., Forestier, G., Weber, J., Idoumghar, L., & Muller, P. (2019). Deep neural network ensembles for time series classification. IEEE International Joint Conference on Neural Networks.

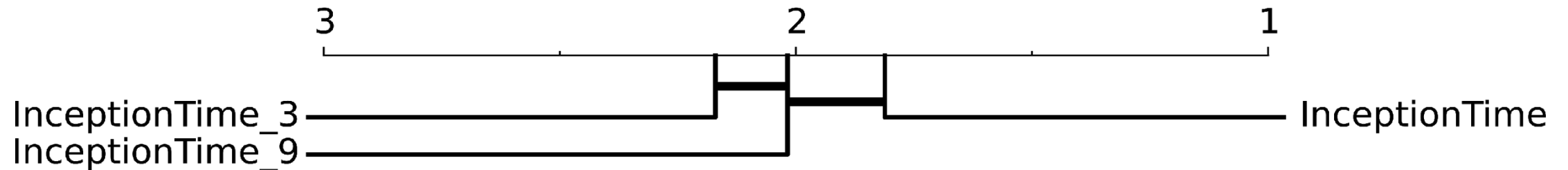


Hyperparameter study: Bottleneck & residual



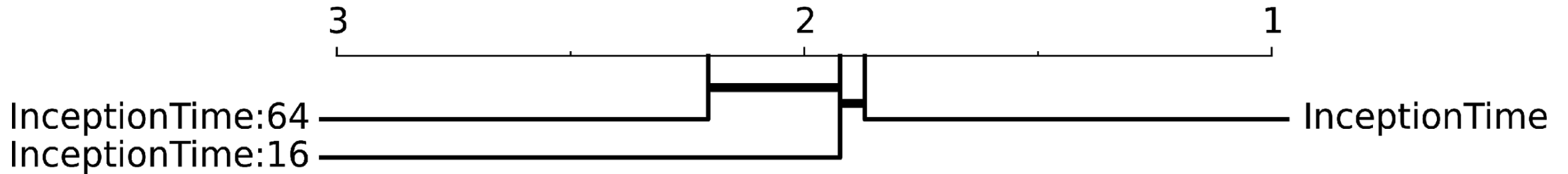
Further investigations ShapeletSim indicated that InceptionTime without the residual connections suffered from a severe overfitting.

Hyperparameter study: depth



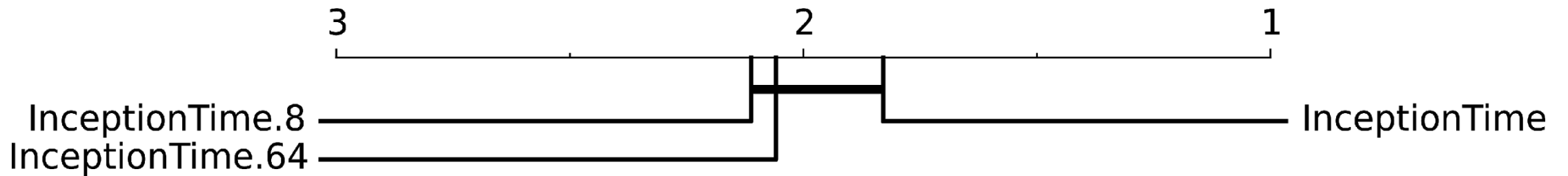
- InceptionTime_x denotes an InceptionTime with x layers
- InceptionTime is equivalent to InceptionTime_6 (the default value)
- A shallower model significantly decreases the accuracy
- A deeper model slightly decreases the accuracy
- Therefore we chose to use a network with 6 layers

Hyperparameter study: number of filters



- InceptionTime:x denotes an InceptionTime with x filters per module
- InceptionTime is equivalent to a model with 32 filters (default value)
- More filters showed a significant decrease in accuracy
- Less filters showed a slight decrease in accuracy
- This hyperparameter affects significantly the complexity of the model

Hyperparameter study: filter length



- InceptionTime.x denotes a model with a filter length equal to x
- InceptionTime is equivalent to a model with a filter length equal to 32
- The default value (32) showed a slight advantage
- Although larger values will produce a larger RF, these experiments showed that this hyperparameter should be carefully chosen

Receptive Field (RF) of a neural network

$$1 + \sum_{i=1}^d (k_i - 1)$$

- d represents the depth of the network
- k_i represents the length of the filters in i^{th} layer
- The stride is considered to be equal to 1
- RF can then be increased by either controlling d or k_i

For images, a large RF is needed to capture more context [1]

1. Luo, W., Li, Y., Urtasun, R., & Zemel, R. (2016). Understanding the effective receptive field in deep convolutional neural networks. In *Advances in neural information processing systems*.

